# GLOBAL POSITIONING SYSTEMS DIRECTORATE SYSTEMS ENGINEERING & INTEGRATION

## INTERFACE SPECIFICATION IS-GPS-705

Navstar GPS Space Segment/User Segment L5 Interfaces

**AUTHENTICATED BY:** 

Michael J. Dunn, DISL, DAF

**Technical Director** 

Global Positioning Systems Directorate

DISTRIBUTION STATEMENT A: Approved for Public Release; Distribution Is Unlimited.

	REVISION RECORD						
LTR	DESCRIPTION	DATE	APPROVED				
NC	Initial Release	24 Nov 03	24 Nov 03				
A	Incorporates GPSIIIA changes	8 Jun 2010	8 Jun 2010				
N/A	SE&I Tech Pubs	29 July 2010					
A	IRN-IS-705A-001 - RFC 00016B - Pseudorandom Noise (PRN) Expansion	21 Sep 2011	8 Dec 2011				
	IRN-IS-705A-002 - RFC 00077B - Public Document Management (GPS III terminology and Space Service Volume (SSV) group delay)						
	IRN-IS-705A-003 - RFC 00086 - User Range Accuracy (URA) Definition						
	IRN-IS-705A-004 - RFC 00091A - Civil Navigation (CNAV) Durations						
	IRN-IS-705A-005 - RFC 00093 - Technical Note 36						
	IRN-IS-705A-006 - RFC 00097 - Pseudorange Parameters						
В	Incorporation of IRN-IS-705A-001 through IRN-IS-705A-006	21 Sep 2011	8 Dec 2011				
	IRN-IS-705B-001	17 Apr 2012	17 Apr 2012				
С	IRN-IS-705B-002 (RFC 139B – Public Signals-in-Space Updates	5 Sep 2012	31 Jan 2013				

## TABLE OF CONTENTS

1	IN	FROL	DUCTION	1
	1.1	Sco	pe	1
	1.2	IS A	Approval and Changes	1
2	AP	PLIC	ABLE DOCUMENTS	1
	2.1	Gov	vernment Documents	1
	2.2	Nor	n-Government Documents.	2
3	RE	QUIF	REMENTS	3
	3.1	Inte	erface Definition.	3
	3.2	Inte	erface Identification.	3
	3.2	2.1	Ranging Codes.	4
	3.2	2.2	NAV Data.	5
	3.2	2.3	L5 Signal Structure.	8
	3.3	Inte	erface Criteria.	8
	3.3	3.1	Composite Signal.	8
	3.3	3.2	PRN Code Characteristics	12
	3.3	3.3	Navigation Data.	18
	3.3	3.4	GPS Time and SV Z-Count.	20
4	NO	Т АР	PLICABLE	.23
5	NO	T AP	PLICABLE	.24
6	NO	TES.		.25
	6.1	Acr	onyms	25
	6.2	Def	initions	27
	6.2	2.1	User Range Accuracy.	27
	6.2	2.2	SV Block Definitions.	27
	6.2	2.3	Operational Interval Definitions.	28

	6.2.4	GPS Week Number.	28
	6.3 Su	pporting Material	28
	6.3.1	L5 Received Signals.	28
	6.3.2	Integrated Phase Noise Characteristics.	28
	6.3.3	Ellipticity Characteristics.	29
	6.3.4	Additional PRN Sequences	29
	6.4 Op	erational Protocols	35
	6.4.1	Lower PRN Numbers Versus Upper PRN Numbers	35
	6.4.2	PRN Number Consistency	35
	6.4.3	PRNs 33 and 37	35
	6.4.4	PRNs 33 through 63	35
10	APPEN	DIX I. LETTERS OF EXCEPTION	36
20	APPEN	DIX II. GPS NAVIGATION DATA STRUCTURE FOR L5 CNAV DATA, $D_5(t)$	41
	20.1	Scope	41
	20.2	Applicable Documents.	41
	20.2.1	Government Documents.	41
	20.2.2	Non-Government Documents.	41
	20.3 I	Requirements	41
	20.3.1	Data Characteristics.	41
	20.3.2	Message Structure.	41
	20.3.3	Message Content.	43
	20.3.4		
	20.3.4	Timing Relationships.	93

## LIST OF FIGURES

Figure 3-1. GPS Space Segment to User Segment Interfaces	3
Figure 3-2. Generation of Codes	13
Figure 3-3. Modulation of Signals	14
Figure 3-4. XA Shift Register Generator Configuration	16
Figure 3-5. XB Shift Register Generator Configuration	17
Figure 3-6. Relative Phases between the XA and XB Sequences	18
Figure 3-7. Convolution Encoder	19
Figure 3-8. Convolution transmit/Decoding Timing Relationships	20
Figure 3-9. Time Line Relationship of a Six-Second Message	22
Figure 6-1. Carrier Phase Noise Spectral Density	29
Figure 10.3-1. Letters of Exception	37
Figure 10.3-2. Letters of Exception (continued)	38
Figure 10.3-3. Letters of Exception (continued)	39
Figure 10.3-4. Letters of Exception (continued)	40
Figure 20-1. Message type 10 - Ephemeris 1	43
Figure 20-2. Message type 11 - Ephemeris 2	44
Figure 20-3. Message type 30 - Clock, IONO & Group Delay	45
Figure 20-4. Message type 31 - Clock & Reduced Almanac	46
Figure 20-5. Message type 32 - Clock & EOP	47
Figure 20-6. Message type 33 - Clock & UTC	48
Figure 20-7. Message type 34 - Clock & Differential Correction	49
Figure 20-8. Message type 35 - Clock & GGTO	50
Figure 20-9. Message type 36 - Clock & Text	51
Figure 20-10. Message Type 37 - Clock & Midi Almanac	52

Figure 20-11. Message type 12 - Reduced Almanac	53
Figure 20-12. Message type 13 - Clock Differential Correction	54
Figure 20-13. Message type 14 - Ephemeris Differential Correction	55
Figure 20-14. Message type 15 - Text	56
Figure 20-15: Sample Application of Correction Parameters	76
Figure 20-16. Reduced Almanac Packet Content	79
Figure 20-17. Differential Correction Data Packet	86

## LIST OF TABLES

Table 3-Ia. Code Phase Assignments (sheet 1 of 2)	5
Table 3-Ia. Code Phase Assignments (sheet 2 of 2)	6
Table 3-Ib. Additional Code Phase Assignments (sheet 1 of 1)	7
Table 3-II. Composite L5 Transmitted Signal Phase**	. 10
Table 3-III. Received Minimum RF Signal Strength	. 10
Table 3-IV. Space Service Volume (SSV) Received Minimum RF Signal Strength for GPS II	Ι
and Subsequent Satellites over the Bandwidth Specified in 3.3.1.1 – GEO Based Antennas	. 10
Table 6-I. Typical Ellipticity vs Angular Range	. 29
Table 6-II. Additional Code Phase Assignments (sheet 1 of 5)	. 31
Table 6-II. Additional Code Phase Assignments (sheet 2 of 5)	. 32
Table 6-II. Additional Code Phase Assignments (sheet 3 of 5)	. 33
Table 6-II. Additional Code Phase Assignments (sheet 4 of 5)	. 34
Table 6-II. Additional Code Phase Assignments (sheet 5 of 5)	. 35
Table 20-I. Message Types 10 and 11 Parameters (1 of 2)	. 62
Table 20-I. Message Types 10 and 11 Parameters (2 of 2)	. 63
Table 20-II. Elements of Coordinate System (part 1 of 2)	. 64
Table 20-II. Elements of Coordinate System (part 2 of 2)	. 65
Table 20-III. Clock Correction and Accuracy Parameters	. 67
Table 20-IV. Group Delay Differential Parameters ****	. 72
Table 20-V. Midi Almanac Parameters	78
Table 20-VI. Reduced Almanac Parameters	. 80
Table 20-VII. Earth Orientation Parameters	. 82
Table 20-VIII. Application of EOP Parameters	. 83
Table 20-IX. UTC Parameters	. 84

Table 20-X. Differential Correction Parameters	87
Table 20-XI. GPS/GNSS Time Offset Parameters	92
Table 20-XII. Message Broadcast Intervals	93

#### 1 INTRODUCTION

- **1.1** <u>Scope.</u> This Interface Specification (IS) defines the requirements related to the interface between the Space Segment (SS) of the Global Positioning System (GPS) and the navigation User Segment (US) of the GPS for radio frequency (RF) link 5 (L5).
- 1.2 <u>IS Approval and Changes.</u> The Interface Control Contractor (ICC) designated by the government is responsible for the basic preparation, obtaining approval coordination, distribution, retention, and Interface Control Working Group (ICWG) coordination of the IS in accordance with GP-03-001. The Navstar GPS Directorate (SMC/GP) is the necessary authority to make this IS effective. SMC/GP administers approvals under the auspices of the Configuration Control Board (CCB), which is governed by the appropriate GPS Directorate Operating Instruction (OI). Military organizations and contractors are represented at the CCB by their respective segment member. All civil organizations and public interest are represented by the Department of Transportation representative of the SMC/GP.

A proposal to change the approved version of this IS can be submitted by any ICWG participating organization to the GPS Directorate and/or the ICC. The ICC is responsible for the preparation of the change paper and change coordination, in accordance with GP-03-001. The ICC prepares the change paper as a Proposed Interface Revision Notice (PIRN) and is responsible for coordination of PIRNs with the ICWG. The ICWG coordinated PIRN must be submitted to the GPS Directorate CCB for review and approval.

The ICWG review period for all Proposed Interface Revision Notices (PIRNs) is 45 days after receipt by individual addressees. A written request to extend the review period may be submitted to the ICC for consideration.

#### 2 APPLICABLE DOCUMENTS

**2.1** Government Documents. The following documents of the issue specified contribute to the definition of the interfaces between the GPS Space Segment and the GPS navigation User Segment (US), and form a part of this IS to the extent specified herein.

Specifications		
Federal		
None		
Military		

Other Government Activity

None

<u>Standards</u>	
Federal	
None	
Military	
None	
Other Publications	
IS-GPS-200 current issue	Navstar GPS Space Segment / Navigation User Interfaces
GP-03-001 current issue	GPS Interface Control Working Group (ICWG) Charter
	e following documents of the issue specified contribute in the GPS SS and the GPS Navigation US and form a in.

None

Other Publications

International Earth Rotation and Reference Systems Service (IERS) Technical Note 36

#### 3 REQUIREMENTS

3.1 <u>Interface Definition.</u> The signal interface between the GPS SS and the GPS Navigation US includes three radio frequency (RF) links: L1, L2 and L5. Figure 3-1 illustrates the interface between the SS and the users. The L5 link is only available on Block IIF and the subsequent Blocks of SVs. Utilizing these links, the space vehicles (SVs) of the SS shall provide continuous earth coverage signals that provide to the users the ranging codes and the system data needed to accomplish the GPS Navigation (NAV) mission. These signals shall be available to a suitably equipped user with RF visibility to an SV, including users in terrestrial and near-terrestrial applications as well as users in orbital applications up to geostationary altitude. The civil functions of the L1 and L2 RF links are specified in IS-GPS-200. Only the L5 link and its relationship with the L1 and L2 links are specified herein.

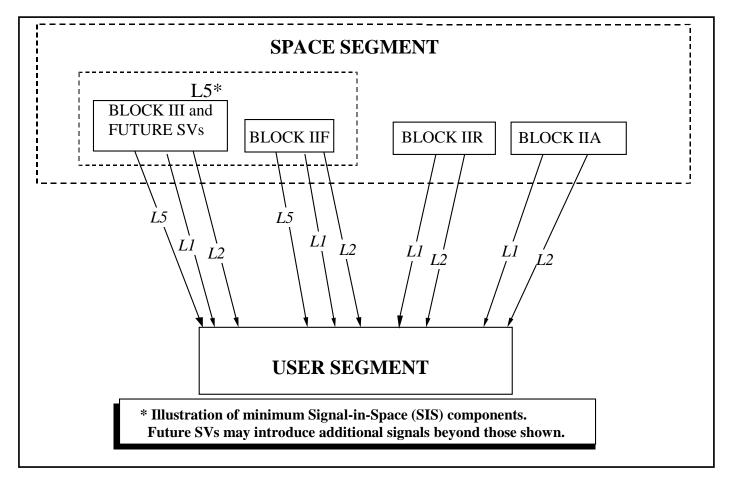


Figure 3-1. GPS Space Segment to User Segment Interfaces

**3.2** <u>Interface Identification.</u> The carriers of the L5 are typically modulated by two bit trains in phase quadrature. One is a composite bit train generated by the modulo-2 addition of a pseudo-random noise (PRN) ranging code, a synchronization sequence (see paragraph 3.3.3.1.2),

and the downlink system data (referred to as L5 CNAV (civil navigation) data), and the second is modulated with a PRN ranging code and synchronization sequence (see paragraph 3.3.2.3) that differ from those used with the L5 CNAV data.

**3.2.1** Ranging Codes. Two PRN ranging codes are transmitted on L5: the in-phase code (denoted as the I5-code); and the quadraphase code (denoted as the Q5-code). Code-division-multiple-access techniques allow differentiating between the SVs even though they may transmit at the same L5 frequency. The SVs shall transmit intentionally "incorrect" versions of the I5 and the Q5-codes when needed to protect the users from receiving and utilizing anomalous NAV signals. These two "incorrect" codes are termed non-standard I5 (NSI5) and non-standard Q5 (NSQ5) codes.

**3.2.1.1** <u>L5-Codes.</u> The PRN ranging codes I5<sub>i</sub>(t) and Q5<sub>i</sub>(t) for SV ID number i are independent, but time synchronized, 1 millisecond in length, with a chipping rate of 10.23 Mbps. For each code, the 1-millisecond sequences are the modulo-2 sum of two sub-sequences referred to as XA and XB<sub>i</sub>; their lengths are 8,190 chips and 8,191 chips, respectively that restart to generate the 10,230 chip code. The XB<sub>i</sub> sequence is selectively advanced, thereby allowing the basic code generation technique to produce different code sequences of 1-millisecond in length. Of these, 32 pairs are currently designated for use by SVs and 5 pairs are currently reserved. Assignment of these code phase segments by SV ID number (or other use) is given in Table 3-I. SV ID and PRN numbers are identical to those for the L1 and L2 signals as specified in IS-GPS-200.

The 74 codes (37 I5-codes and 37 Q5-codes) are a selected subset of over 4,000 possible codes that could be generated using the selective advance. The remaining codes are available for future use of additional SVs and/or other L5 signal applications such as Satellite-Based Augmentation System (SBAS) satellite signals. Of the remaining codes, Section 6.3.4 provides a selected subset of codes with assigned PRN numbers.

4

**3.2.1.2** <u>Non-Standard Codes.</u> The NSI5 and NSQ5 codes, used to protect the user from tracking anomalous navigation signals are not for utilization by the user and, therefore, are not defined in this document. The SVs shall also be capable of initiating and terminating the broadcast of NSI5 and/or NSQ5 code(s) independently of each other, in response to Control Segment (CS) command.

**3.2.2** NAV Data. The L5 CNAV data,  $D_5(t)$ , includes SV ephemerides, system time, SV clock behavior data, status messages and C/A to P (or Y) code handover information, etc. The 50 bps data is encoded in a rate 1/2 convolution encoder. The resulting 100 symbols per second (sps) symbol stream is modulo-2 added to the I5-code only; the resultant bit-train is used to modulate the L5 in-phase (I) carrier. The content and characteristics of the L5 CNAV data,  $D_5(t)$ , are given in Appendix II of this document. In general, the data content is very similar to that modulated on the L2 C channel of the SV.

The L5 quadraphase (Q5) carrier has no data.

	Table 3-Ia	a. Code Phase Ass	signments (sheet 1 of 2	)	
GPS PRN	XB Code Ad	vance – Chips*	nitial XB Code State**		
Signal No.	I5	Q5	I5	Q5	
1	266	1701	0101011100100	1001011001100	
2	365	323	1100000110101	0100011110110	
3	804	5292	010000001000	1111000100011	
4	1138	2020	1011000100110	0011101101010	
5	1509	5429	1110111010111	0011110110010	
6	1559	7136	0110011111010	0101010101001	
7	1756	1041	1010010011111	1111110000001	
8	2084	5947	1011110100100	0110101101000	
9	2170	4315	1111100101011	1011101000011	
10	2303	148	0111111011110	0010010000110	
11	2527	535	0000100111010	0001000000101	
12	2687	1939	1110011111001	0101011000101	
13	2930	5206	0001110011100	0100110100101	
14	3471	5910	0100000100111	1010000111111	
15	3940	3595	0110101011010	1011110001111	
16	4132	5135	0001111001001	1101001011111	
17	4332	6082	0100110001111	1110011001000	
18	4924	6990	1111000011110	1011011100100	
19	5343	3546	1100100011111	0011001011011	

<sup>\* -</sup> XB Code Advance is the number of XB clock cycles beyond an initial state of all 1s.

NOTE: The code phase assignments constitute inseparable pairs, each consisting of a specific I5 and a specific Q5-code phase, as shown above.

<sup>\*\*</sup> In the binary notation for the first 13 chips of the I5 and Q5 XB codes as shown in these columns. The rightmost bit is the first bit out. Since the initial state of the XA Code is all 1s, these first 13 chips are also the complement of the initial states of the I5 or Q5-codes.

Table 3-Ia. Code Phase Assignments (sheet 2 of 2)					
GPS PRN	XB Code Ad	XB Code Advance – Chips* Initial XB Code State**			
Signal No.	I5	Q5	I5	Q5	
20	5443	1523	0110101101101	1100001110001	
21	5641	4548	0010000001000	0110110010000	
22	5816	4484	1110111101111	0010110001110	
23	5898	1893	1000011111110	1000101111101	
24	5918	3961	1100010110100	0110111110011	
25	5955	7106	1101001101101	0100010011011	
26	6243	5299	1010110010110	01010101111100	
27	6345	4660	0101011011110	1000011111010	
28	6477	276	01111010101110	1111101000010	
29	6518	4389	0101111100001	0101000100100	
30	6875	3783	1000010110111	1000001111001	
31	7168	1591	0001010011110	0101111100101	
32	7187	1601	0000010111001	1001000101010	
33	7329	749	1101010000001	1011001000100	
34	7577	1387	1101111111001	1111001000100	
35	7720	1661	1111011011100	0110010110011	
36	7777	3210	1001011001000	0011110101111	
37	8057	708	0011010010000	0010011010001	

<sup>\*</sup> XB Code Advance is the number of XB clock cycles beyond an initial state of all 1s.

NOTE: The code phase assignments constitute inseparable pairs, each consisting of a specific I5 and a specific Q5-code phase, as shown above.

<sup>\*\*</sup> In the binary notation for the first 13 chips of the I5 and Q5 XB codes as shown in these columns. The rightmost bit is the first bit out. Since the initial state of the XA Code is all 1s, these first 13 chips are also the complement of the initial states of the I5 or Q5-codes.

PRN	XB Code Advance – Chips**  Initial XB Code State***		Code State***	
Signal No.*	I5	Q5	I5	Q5
38	5358	4226	0101100000110	1111110011101
39	3550	5604	1001001100101	0101010011111
40	3412	6375	1100111001010	1000110101010
41	819	3056	0111011011001	0010111100100
42	4608	1772	0011101101100	1011000100000
43	3698	3662	0011011111010	0011001011001
44	962	4401	1001011010001	1000100101000
45	3001	5218	1001010111111	0000001111110
46	4441	2838	0111000111101	000000010011
47	4937	6913	0000001000100	0101110011110
48	3717	1685	1000101010001	0001001000111
49	4730	1194	0011010001001	0011110000100
50	7291	6963	1000111110001	0100101011100
51	2279	5001	1011100101001	0010100011111
52	7613	6694	0100101011010	1101110011001
53	5723	991	0000001000010	0011111101111
54	7030	7489	0110001101110	1100100110111
55	1475	2441	0000011001110	1001001100110
56	2593	639	1110111011110	0100010011001
57	2904	2097	0001000010011	000000001011
58	2056	2498	0000010100001	0000001101111
59	2757	6470	0100001100001	0101101101111
60	3756	2399	0100101001001	0100100001101
61	6205	242	0011110011110	1101100101011
62	5053	3768	1011000110001	1010111000100
63	6437	1186	0101111001011	0010001101001

<sup>\*</sup> PRN sequences 38 through 63 are reserved for GPS.

NOTE #1: The code phase assignments constitute inseparable pairs, each consisting of a specific I5 and a specific Q5-code phase, as shown above.

NOTE #2: PRNs 38-63 are required per this Table if a manufacturer chooses to include these PRNs in their receiver design.

<sup>\*\*</sup> XB Code Advance is the number of XB clock cycles beyond an initial state of all 1s.

<sup>\*\*\*</sup> In the binary notation for the first 13 chips of the I5 and Q5 XB codes as shown in these columns. The rightmost bit is the first bit out. Since the initial state of the XA Code is all 1s, these first 13 chips are also the complement of the initial states of the I5 or Q5-codes.

- **3.2.3** <u>L5 Signal Structure.</u> The L5 consists of two carrier components that are in phase quadrature with each other. Each carrier component is bi-phase shift key (BPSK) modulated by a separate bit train. One bit train is the modulo-2 sum of the I5-code, NAV data, and synchronization sequence while the other is the Q5-code with no NAV data, but with another synchronization sequence. For a particular SV, all transmitted signal elements (carriers, codes, synchronization sequences, and data) are coherently derived from the same on-board frequency source.
- **3.3** <u>Interface Criteria.</u> The criteria specified in the following define the requisite characteristics of the L5 interface.
- **3.3.1** <u>Composite Signal.</u> The following criteria define the characteristics of the composite L5 signal.
- **3.3.1.1** Frequency Plan. The requirements specified in this document shall pertain to the signal contained within a 24 MHz band centered about the L5 nominal frequency. The carrier frequencies for the L1, L2 and L5 signals shall be coherently derived from a common frequency source within the SV. The nominal frequency of this source -- as it appears to an observer on the ground -- is 10.23 MHz. The SV carrier frequency and clock rates -- as they would appear to an observer located in the SV -- are offset to compensate for relativistic effects. The clock rates are offset by  $\Delta f/f = -4.4647E-10$ , equivalent to a change in the I5 and Q5-code chipping rate of 10.23 MHz offset by a  $\Delta f = -4.5674E-3$  Hz. This is equal to 10.2299999954326 MHz. The nominal carrier frequency ( $f_0$ ) -- as it appears to an observer on the ground shall be 1176.45 MHz, or 115 times 10.23 MHz.
- **3.3.1.2** Correlation Loss. Correlation loss is defined as the difference between the SV power received in the bandwidth defined in 3.3.1.1 (excluding signal combining loss) and the signal power recovered in an ideal correlation receiver of the same bandwidth using an exact replica of the waveform within an ideal sharp-cutoff filter bandwidth centered at L5, whose bandwidth corresponds to that specified in 3.3.1.1 and whose phase is linear over that bandwidth. The correlation loss apportionment due to SV modulation and filtering imperfections shall be 0.6 dB maximum.
- **3.3.1.3** Carrier Phase Noise. The phase noise spectral density of the un-modulated carrier shall be such that a phase locked loop of 10 Hz one-sided noise bandwidth shall be able to track the carrier to an accuracy of 0.1 radians root mean square (RMS). See additional supporting material for phase noise characteristics in section 6.3.2.
- **3.3.1.4 Spurious Transmissions.** In-band spurious transmissions, from the SV, shall be at or below -40 dBc over the band specified in 3.3.1.1. In-band spurious transmissions are defined as

transmissions within the band specified in 3.3.1.1 which are not expressly components of the L5 signal.

**3.3.1.5** Phase Quadrature. The two L5 carrier components modulated by the two separate bit trains (I5-code plus data and Q5-code with no data) shall be in phase quadrature (within  $\pm 100$  milliradians) with the Q5 signal carrier lagging the I5 signal by 90 degrees. Referring to the phase of the I5 carrier when I5<sub>i</sub>(t) equals zero as the "zero phase angle," the I5 and Q5-code generator output shall control the respective signal phases in the following manner: when I5<sub>i</sub>(t) equals one, a 180-degree phase reversal of the I5-carrier occurs; when Q5<sub>i</sub>(t) equals one, the Q5 carrier advances 90 degrees; when the Q5<sub>i</sub>(t) equals zero, the Q5 carrier shall be retarded 90 degrees (such that when Q5<sub>i</sub>(t) changes state, a 180-degree phase reversal of the Q5 carrier occurs). The resultant nominal composite transmitted signal phases as a function of the binary state of the modulating signals are as shown in Table 3-II.

**3.3.1.6** <u>Signal Power Levels.</u> The SV shall provide, at a minimum, worst-case I5 and Q5 navigation signal strength at end-of-life (EOL), in order to meet the levels specified in Table 3-III. The minimum received power is measured at the output of a 3 dBi linearly polarized user receiving antenna (located near ground) at worst normal orientation, when the SV is above a 5-degree elevation angle. The received signal levels are observed within the in-band allocation defined in paragraph 3.3.1.1. Additional related data is provided as supporting material in paragraph 6.3.1.

The GPS III SV shall provide L5 signals with the following characteristic: the L5 off-axis relative power (referenced to peak transmitted power) shall not decrease by more than 2 dB from the Edge-of-Earth (EOE) to nadir, and no more than 18 dB from EOE to 26 degrees off nadir; the power drop off between EOE and  $\pm 26$  degrees shall be in a monotonically decreasing fashion.

Table 3-II. Composite L5 Transmitted Signal Phase**		
Nominal Composite L5 Signal Phase*	Code State	
	15	Q5
0°	0	0
-90°	1	0
+90°	0	1
180°	1	1

<sup>\*</sup> Relative to 0, 0 code state with positive angles leading and negative angles lagging.

<sup>\*\*</sup> Based on the composite of two L5 carrier components at the same power.

Table 3-III. Received Minimum RF Signal Strength		
SV	Signal	
	15	Q5
Block IIF	-157.9 dBW	-157.9 dBW
GPS III	-157.0 dBW	-157.0 dBW

**3.3.1.6.1** Space Service Volume (SSV) Received Signal Power Levels. The SV shall provide, at a minimum, worst-case I5 and Q5 navigation signal strength at end-of-life (EOL), in order to meet the SSV levels specified in Table 3-IV. The minimum received power is measured at the output of a 0 dBi right-hand circularly polarized (i.e. 0 dB axial ratio) user receiving antenna at normal orientation at the off-nadir angle of 26.0 degrees. The received signal levels are observed within the in-band allocation defined in paragraph 3.3.1.1.

Table 3-IV. Space Service Volume (SSV) Received Minimum RF Signal Strength for GPS III and Subsequent Satellites over the Bandwidth Specified in 3.3.1.1 – GEO Based Antennas		
SV	Signal	
	I5	Q5
GPS III and	-182.0 dBW	-182.0 dBW
Subsequent Blocks		

- **3.3.1.7** Equipment Group Delay. Equipment group delay is defined as the delay between the signal radiated output of a specific SV (measured at the antenna phase center) and the output of that SV's on-board frequency source; the delay consists of a bias term and an uncertainty. The bias term on L1/L2 P(Y) is of no concern to users since it is included in the clock correction parameters relayed in the NAV data, and is therefore accounted for by user computations of system time (reference paragraphs 20.3.3.2.3, 20.3.3.2.3 and 20.3.3.3.2.4). The uncertainty (variation) of these delays as well as the group delay differential between the signals of L1, L2, and L5 are defined in the following.
- **3.3.1.7.1 Group Delay Uncertainty.** The effective uncertainty of the group delays shall not exceed 3.0 nanoseconds (95% probability).
- **3.3.1.7.2** Group Delay Differential. The group delay differential between the radiated L1 and L5 signals (i.e. L1 P(Y) and L5 I5; and L1 P(Y) and L5 Q5) is specified as consisting of random plus bias components. The mean differential is defined as the bias component and will be either positive or negative. For a given navigation payload redundancy configuration, the absolute value of the mean differential delay shall not exceed 30.0 nanoseconds. The random plus non-random variations about the mean shall not exceed 3.0 nanoseconds (95% probability), when including consideration of the temperature and antenna effects during a vehicle orbital revolution. L1 and L2 group delay differential is described in 3.3.1.7.2 of IS-GPS-200. Corrections for the bias components of the group delay differential are provided to the users in the NAV message using parameters designated as T<sub>GD</sub> (reference paragraph 20.3.3.3.3.2 of IS-GPS-200) and Inter-Signal Correction (ISC) (reference paragraph 20.3.3.3.1.2).
- **3.3.1.7.3** Space Service Volume Group Delay Differential. The group delay differential between the radiated L5 signal, with respect to the Earth Coverage signal, for users of the Space Service Volume are provided in <a href="http://www.igs.org/products/ssv">http://www.igs.org/products/ssv</a>.

- **3.3.1.8** <u>Signal Coherence.</u> All transmitted signals on the same carrier for a particular SV shall be coherently derived from the same on-board frequency standard. On the L5 channel, the chip transitions of the two modulating signals, L5I and L5Q, shall be such that the average time difference between them, and between each and the transitions of L1 P(Y), do not exceed 10 nanoseconds. The variable time difference shall not exceed 1 nanosecond (95% probability), when including consideration of the temperature and antenna effect changes during a vehicle orbital revolution. Corrections for the bias components of the group delay differential are provided to the users using parameters designated as ISCs (reference paragraph 20.3.3.3.1.2).
- **3.3.1.9** Signal Polarization. The transmitted signal shall be right-hand circularly polarized (RHCP). For the angular range of  $\pm 13.8$  degrees from nadir, L5 ellipticity shall be no worse than 2.4 dB. Nominal values are listed in section 6.3.3.
- **3.3.2 PRN Code Characteristics.** The characteristics of the I5-codes and the Q5-codes are defined below in terms of their structure and the basic method used for generating them. Figures 3-2 and 3-3 depict simplified block diagrams of the scheme for generating the 10.23 Mbps  $I5_i(t)$  and  $Q5_i(t)$  patterns, and for modulo-2 summing the I5 patterns with the NAV bit train,  $D_5(t)$ , which is rate 1/2 encoded and clocked at 100 sps. In addition, the 100 sps are modulated with a 10-bit Neuman-Hofman code that is clocked at 1 kHz. The resultant composite bit trains are then used to modulate the L5 in-phase carrier. The Q5-code is modulated with a 20-bit Neuman-Hofman code that is also clocked at 1 kHz.
- **3.3.2.1** Code Structure. The  $I5_i(t)$  pattern (I5-code) and the  $Q5_i(t)$  pattern (Q5-code) are both generated by the modulo-2 summation of two PRN codes, XA(t) and  $XBI_i(nI_i, t)$  or  $XBQi(nQ_i, t)$ , where nIi and nQ<sub>i</sub> are initial states of  $XBI_i$  and  $XBQ_i$  for satellite i. There are over 4000 unique L5 codes generated using different initial states of which 128 are currently assigned and identified in Table 3-Ia and Table 3-Ib using the same basic code generator. Section 6.3.4 provides a selected subset of additional L5-code sequences with assigned PRN numbers.

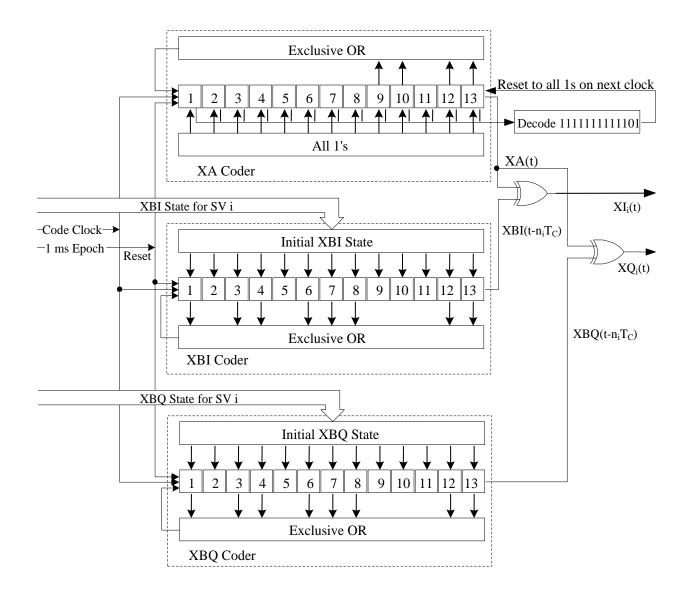


Figure 3-2. Generation of Codes

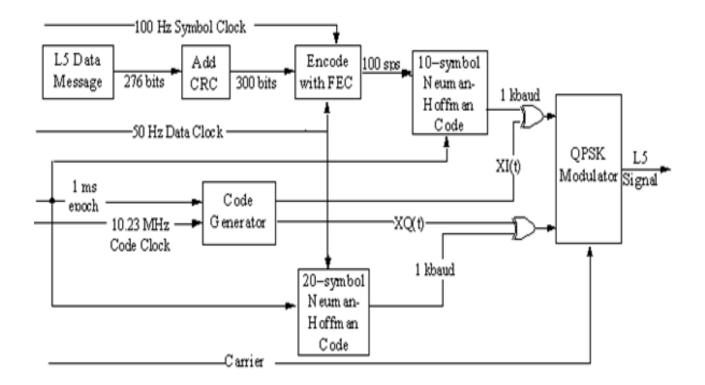


Figure 3-3. Modulation of Signals

**3.3.2.2** <u>Code Generation.</u> Each I5<sub>i</sub>(t) pattern (I5-code) and Q5<sub>i</sub>(t) pattern (Q5-code) are the modulo-2 sum of two extended patterns clocked at 10.23 Mbps (XA and XBI<sub>i</sub> or XBQ<sub>i</sub>). XA is an 8190 length code, with an initial condition of all 1s, that is short cycled 1-chip before its natural conclusion and restarted to run over a period of 1 millisecond (synchronized with the L1 frequency C/A-code) for a total of 10,230 chips. The XBI<sub>i</sub> and XBQ<sub>i</sub>, with initial conditions indicated in Table 3-I, are 8191 length codes that are not short cycled. They are restarted at their natural completion and run over a period of 1 millisecond (synchronized with the XA code) for a total of 10,230 chips. The polynomials for XA and XBI<sub>i</sub> or XBQ<sub>i</sub> codes, as referenced to the shift register input, are:

XA: 
$$1 + x^9 + x^{10} + x^{12} + x^{13}$$
, and   
XBI<sub>i</sub> or XBQ<sub>i</sub>:  $1 + x + x^3 + x^4 + x^6 + x^7 + x^8 + x^{12} + x^{13}$ .

Samples of the relationship between shift register taps and the exponents of the corresponding polynomial, referenced to the shift register input, are as shown in Figures 3-4 (XA code) and 3-5 (XB code). In the case of the XB codes, the shift register can either be initialized with all 1s and advanced n<sub>i</sub> states as specified in Table 3-I, or initialized with the state indicated in Table 3-I.

The state of each generator can be expressed as a code vector word which specifies the binary sequence constant of each register as follows:

- (a) the vector consists of the binary state of each stage of the register,
- (b) the stage 13 value appears at the right followed by the values of the remaining states in order of descending stage numbers, and
- (c) the shift direction is from lower to higher stage number with stage 13 providing the current output. This code vector convention represents the present output and 12 future outputs in sequence. Using this convention, at each XA epoch (state 8190), the XA shift register is initialized to the code vector 111111111111111, while at each XB epoch (state 8191), the XB shift register is initialized to a code vector peculiar to the PRN number and phase. The XB code vectors are as indicated in Table 3-I. Alternatively, the XB shift register is initialized to the code vector 111111111111111 and advanced  $n_i$  states as indicated in Table 3-I.

The natural 8191 chips of the XA sequence is shortened to 8190 chips to cause precession of the second XA sequence with respect to the natural 8191 chip XB sequence, as shown in Figure 3-6. Re-initialization of the XA shift register produces a 10230-chip sequence by omitting the last 6151 chips of the second natural XA sequence, or reinitializing to all 1s at the 1 ms epoch. The XB shift register is simply allowed to run its natural course until the next 1 ms epoch when it is reinitialized at its initial state, B0, based upon PRN number and phase. This results in the phase of the XB sequence leading by one chip during the second XA sequence in the 1-millisecond period. Depending upon the initial state of the XB sequence, a third 8191-chip sequence may be started before the 10230-chip sequence is completed. Two different scenarios that may result are shown in Figure 3-6.

In scenario a, the initial state of the XB sequence, B0, is less than State 6152. Thus, the second natural XB sequence does not run to completion prior to the next 1 ms epoch. In scenario b, the initial state of the XB sequence, B0, is greater than State 6151. Thus, the second natural XB sequence runs to completion and a third natural sequence starts (except when B0 is State 6152) prior to the next 1 ms epoch.

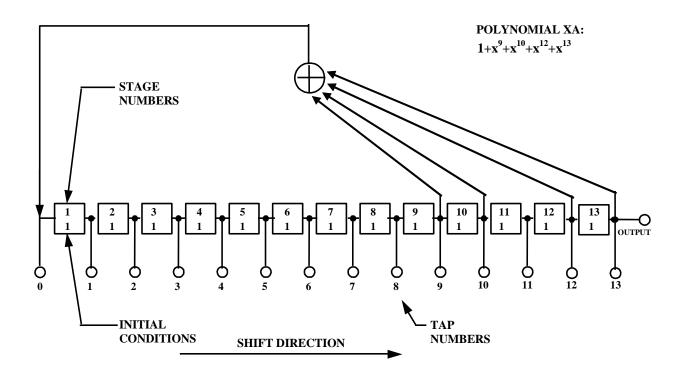


Figure 3-4. XA Shift Register Generator Configuration

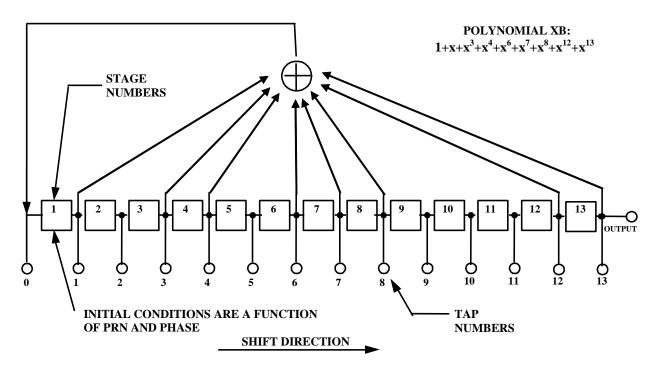


Figure 3-5. XB Shift Register Generator Configuration

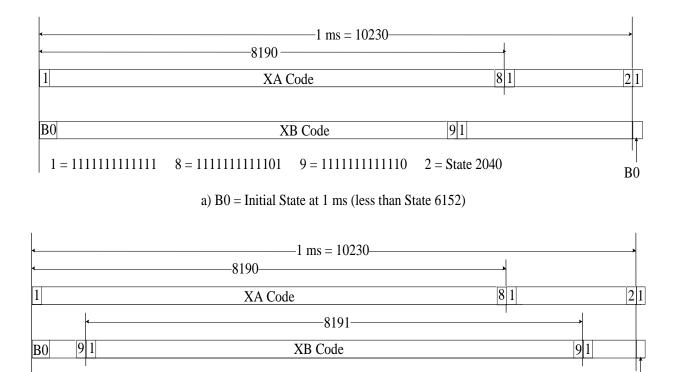


Figure 3-6. Relative Phases between the XA and XB Sequences

b) B0 = Initial State at 1 ms (greater than State 6151)

9 = 1111111111110

2 = State 2040

**3.3.2.3 Q5 Synchronization Sequence.** Each of the 1 ms Q5-code blocks is further encoded with a 20-bit Neuman-Hofman code. The 20 bits are modulo-2 added to the Q5 code chips at the PRN code epoch rate of 1 kHz. The code, nh20(t), starting coincident with the 20 ms data epoch on the I5 channel, is as follows:

$$1^{st} \hspace{1cm} Last$$
 
$$nh20(t) = 0\ 0\ 0\ 0\ 1\ 0\ 0\ 1\ 1\ 0\ 1\ 0\ 1\ 0\ 1\ 1\ 0$$

#### 3.3.3 Navigation Data.

1 = 111111111111111

**3.3.3.1** Navigation Data Modulation. The L5 CNAV bit train,  $D_5(t)$ , is rate 1/2 convolution encoded and, thus, clocked at 100 symbols per second (sps). In addition, the 100 sps symbols are modulated with a 10-bit Neuman-Hofman code that is clocked at 1 kHz (reference paragraph 3.3.3.1.2). The resultant symbol sequence is then modulo-2 added with I5 PRN code and used to modulate the L5 in-phase carrier.

B0

**3.3.3.1.1** Forward Error Correction. The L5 CNAV bit train, D<sub>5</sub>(t), will always be rate 1/2 convolution encoded with a Forward Error Correction (FEC) code. Therefore, the symbol rate is 100 sps. The convolution coding will be constraint length 7, with a convolution encoder logic arrangement as illustrated in Figure 3-7. The G1 symbol is selected on the output as the first half of a 20-millisecond data bit period coincident with the first bit of the 20-bit Q5 Neuman-Hofman code.

Six-second navigation messages broadcast by the SV are synchronized with every fourth of the SV's P(Y)-code X1 epochs. Although these epochs are not necessarily accessible to the L5 user, they are used within the SV to define GPS time. However, message synchronization does provide the L5 user an access to the time of every 4<sup>th</sup> P(Y)-code X1 epoch. The navigation message is FEC encoded in a continuous process independent of message boundaries (i.e. at the beginning of each new message, the encoder registers illustrated in Figure 3-7 contain the last six bits of the previous message). Thus, herein, reference will continue to be made to these X1 epochs. See IS-GPS-200 for details.

The FEC encoding convolves successive messages. It is necessary to define which transmitted symbol is synchronized to SV time as follows. The beginning of the first symbol that contains any information about the first bit of a message will be synchronized to every fourth X1 epoch (referenced to end/start of week). The users' convolution decoders will introduce a fixed delay that depends on their respective algorithms (usually 5 constraint lengths, or 35 bits), for which they must compensate to determine system time from the received signal. This convolution decoding delay and the various relationships with the start of the data block transmission and SV timing are illustrated in Figure 3-8 for the L5 signal.

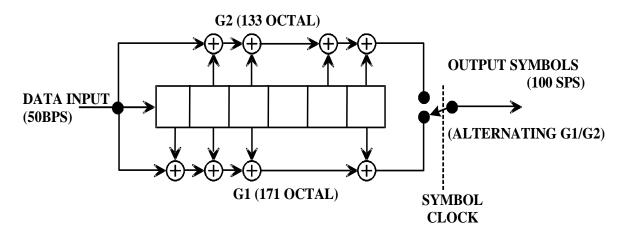


Figure 3-7. Convolution Encoder

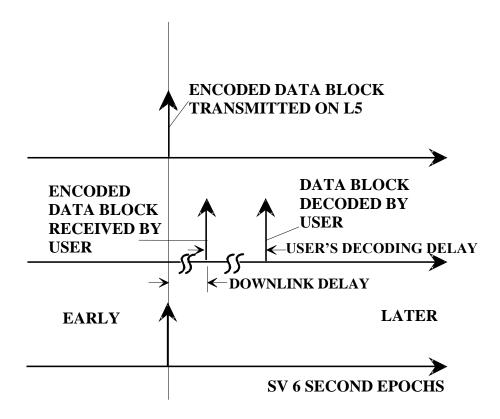


Figure 3-8. Convolution Transmit/Decoding Timing Relationships

**3.3.3.1.2** Neuman-Hofman Code. Each of the 100 sps symbols are further encoded with a 10-bit Neuman-Hofman code. The 10-bit Neuman-Hofman code is defined to be 0000110101. The 10 bits are modulo-2 added to the symbols at the PRN code epoch rate of 1 kHz starting at the 100 sps symbol transitions. The result is that a "1" data symbol is replaced by 1111001010, and a "0" data symbol is replaced by 0000110101.

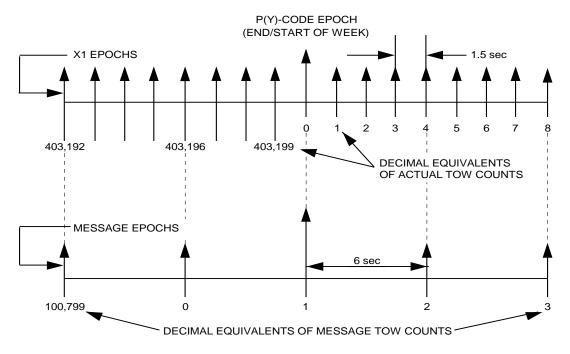
**3.3.4** GPS Time and SV Z-Count. GPS time is established by the Operational Control System (OCS) and is referenced to Coordinated Universal Time (UTC) as maintained by the U.S. Naval Observatory (UTC (USNO)) zero time-point defined as midnight on the night of January 5, 1980/morning of January 6, 1980. GPS time is the ensemble of corrected composite L1/L2 P(Y) SV times, corrected via the clock corrections in the L1 and L2 NAV data and the relativity correction. The largest unit used in stating GPS time is one week defined as 604,800 seconds, concatenated with the GPS week number. GPS time may differ from UTC because GPS time is a continuous time scale, while UTC is corrected periodically with an integer number of leap seconds. There also is an inherent but bounded drift rate between the UTC and GPS time scales. The OCS controls the GPS time scale to be within one microsecond of UTC (modulo one second).

The L5 CNAV data contains the requisite data for relating GPS time to UTC. The accuracy of this data during the transmission interval will be such that it relates GPS time to UTC (USNO) to

within 20.0 nanoseconds (one sigma). This data is generated by the CS (or provided to the CS); therefore, the accuracy of these relationships may degrade if for some reason the CS is unable to upload data to an SV.

In each SV the X1 epochs of the P-code offer a convenient unit for precisely counting and communicating time. Time stated in this manner is referred to as Z-count, which is given as a binary number consisting of two parts as follows:

- a. The binary number represented by the 19 least significant bits of the Z-count is referred to as the time of week (TOW) count and is defined as being equal to the number of X1 epochs that have occurred since the transition from the previous week. The count is short-cycled such that the range of the TOW-count is from 0 to 403,199 X1 epochs (equaling one week) and is reset to zero at the end of each week. The TOW-count's zero state is defined as that X1 epoch which is coincident with the start of the present week. This epoch occurs at (approximately) midnight Saturday night-Sunday morning, where midnight is defined as 0000 hours on the UTC scale, which is nominally referenced to the Greenwich Meridian. Over the years the occurrence of the "zero state epoch" may differ by a few seconds from 0000 hours on the UTC scale since UTC is periodically corrected with leap seconds while the TOW-count is continuous without such correction. A truncated version of the TOW-count, consisting of its 17 most significant bits, is contained in each of the six-second messages of the L5 downlink data stream; the relationship between the actual TOW-count and its truncated message version is illustrated by Figure 3-9.
- b. The most significant bits of the Z-count are a binary representation of the sequential number assigned to the current GPS week (see paragraph 6.2.4).



#### NOTES:

- 1. THE TOW COUNT APPEARS IN EACH 6-SECOND MESSAGE
- 2. THE 6-SECOND MESSAGE TOW COUNT CONSISTS OF THE 17 MSBs OF THE ACTUAL TOW COUNT AT THE START OF THE NEXT MESSAGE.
- 3. TO CONVERT FROM THE MESSAGE TOW COUNT TO THE ACTUAL TOW COUNT AT THE START OF THE NEXT MESSAGE, MULTIPLY BY FOUR.

Figure 3-9. Time Line Relationship of a Six-Second Message

## 4 NOT APPLICABLE

23

### 5 NOT APPLICABLE

## 6 NOTES

## 6.1 Acronyms

AFMC	-	Air Force Materiel Command
AFSPC	-	Air Force Space Command
ASCII	-	American Standard Code for Information Interchange
bps	-	bits per second
BPSK	-	Bi-Phase Shift Key
C/A	-	Course/Acquisition
CDC	-	Clock Differential Correction
CNAV	-	Civil Navigation
CRC	-	Cyclic Redundancy Check
CS	-	Control Segment
dB	-	Decibel
dBc	-	Power ratio of a signal to a (unmodulated) carrier signal, expressed in decibels
dBi	-	Decibels with respect to isotropic antenna
dBW	-	Decibels with respect to 1 Watt
DC	-	Differential Correction
DoD	-	Department of Defense
ECEF	-	Earth-Centered, Earth-Fixed
ECI	-	Earth Centered Inertial
EDC	-	Ephemeris Differential Correction
EOL	-	End of Life
FEC	-	Forward Error Correction
GGTO	-	GPS/GNSS Time Offset
GNSS	-	Global Navigation Satellite System
GPS	-	Global Positioning System

GPSW	-	Global Positioning System Wing
Hz	-	Hertz
I5	-	In-phase Code on L5 Signal
ICC	-	Interface Control Contractor
ID	-	Identification
IODC	-	Issue of Data, Clock
IS	-	Interface Specification
ISC	-	Inter-Signal Correction
LSB	-	Least Significant Bit
MSB	-	Most Significant Bit
NAV	-	Navigation
NSI5	-	Non-Standard I-Code
NSQ5	-	Non-Standard Q-Code
OCS	-	Operational Control System
PIRN	-	Proposed Interface Revision Notice
PRN	-	Pseudo-Random Noise
P(Y)	-	Precise (Anti-Spoof) Code
Q5	-	Quadraphase code on L5 Signal
RF	-	Radio Frequency
RHCP	-	Right Hand Circular Polarization
RMS	-	Root Mean Square
SBAS	-	Satellite Based Augmentation System
sps	-	Symbols per Second.
SIS	-	Signal In Space
SS	-	Space Segment
SSV	-	Space Service Volume
SV	-	Space Vehicle

TBD	-	To Be Determined
TBS	-	To Be Supplied
TOW	-	Time Of Week
URA	-	User Range Accuracy
US	-	User Segment
USNO	-	US Naval Observatory
UTC	-	Coordinated Universal Time
WGS 84	-	World Geodetic System 1984
WN	-	Week Number
WN <sub>e</sub>	-	Extended Week Number

#### 6.2 <u>Definitions.</u>

- **6.2.1** User Range Accuracy. See Section 6.2.1 of IS-GPS-200.
- **6.2.2 SV Block Definitions.** The following block definitions are given to facilitate discussion regarding the capability of the various blocks of GPS satellites to support the SV-to-user interface.
- **6.2.2.1 Developmental SVs.** See paragraph 6.2.2.1 of IS-GPS-200.
- **6.2.2.2 Operational SVs.** The operational satellites are designated Block IIA, Block IIR, Block IIRM, Block IIF and GPS III SVs. Characteristics of these SVs are provided below. These SVs transmit configuration codes as specified in paragraph 20.3.3.5.1.4 of IS-GPS-200. The navigation signal provides no direct indication of the type of the transmitting SV.
- **6.2.2.2.1** <u>Block II SVs.</u> See paragraph 6.2.2.2.1 of IS-GPS-200. These satellites do not broadcast the L5 signal.
- **6.2.2.2.2 Block IIA SVs.** See paragraph 6.2.2.2.2 of IS-GPS-200. These satellites do not broadcast the L5 signal.
- **6.2.2.2.3 Block IIR SVs.** See paragraph 6.2.2.2.3 of IS-GPS-200. These satellites do not broadcast the L5 signal.
- **6.2.2.2.4 Block IIR-M SVs.** See paragraph 6.2.2.2.4 of IS-GPS-200. These satellites do not broadcast the L5 signal.

27

- **6.2.2.2.5 Block IIF SVs.** See paragraph 6.2.2.2.5 of IS-GPS-200. The IIF operational SVs do broadcast the L5 signal.
- **6.2.2.2.6 GPS III SVs.** See paragraph 6.2.2.2.6 of IS-GPS-200. The III operational SVs do broadcast the L5 signal.
- **6.2.3 Operational Interval Definitions.** See paragraph 6.2.3 of IS-GPS-200. There is no requirement for extended operations on L5.
- **6.2.4 GPS Week Number.** See paragraph 6.2.4 of IS-GPS-200 and paragraph 20.3.3.1.1.1.

#### **6.3** Supporting Material.

- **6.3.1 L5 Received Signals.** The guaranteed minimum user-received signal levels are defined in paragraph 3.3.1.6. Higher received signal levels can be caused by such factors as SV attitude errors, mechanical antenna alignment errors, transmitter power output variations resultant of temperature variations, voltage variations and power amplifier variations, and a variability in link atmospheric path loss. In addition and for the purpose of establishing GPS user receiver dynamic range, the maximum received signal level, as measured at the output of a 3 dBi linearly polarized receiver antenna, is not expected to exceed -150.0 dBW in each L5 signal channel.
- **6.3.2** <u>Integrated Phase Noise Characteristics.</u> As an aid to user equipment receiver designers, a plot is provided (Figure 6-1) of a typical GPS Block IIF phase noise spectral density for the un-modulated L5 carrier. A plot of a typical GPS III phase noise spectral density will be added TBD.

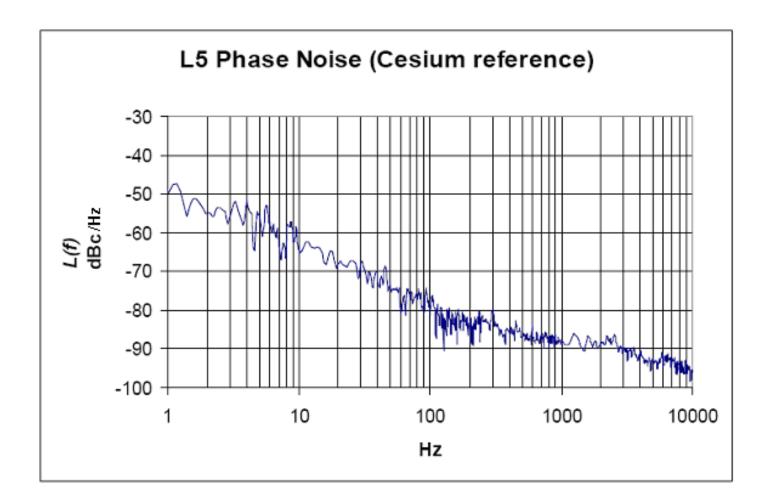


Figure 6-1. Carrier Phase Noise Spectral Density

**6.3.3** <u>Ellipticity Characteristics.</u> As an aid to user equipment receiver designers, a table is provided (Table 6-I) of a typical GPS Block IIF ellipticity as a function of angular range. A table of a typical GPS III ellipticity will be added TBD.

Table 6-I. Typical Ellipticity vs Angular Range

Angle (deg)	±0	±2	±4	±6	±8	±10	±12	±14.3
Ellipticity (dB)	1.5	1.5	1.5	1.5	1.5	1.5	1.5	2.0

**6.3.4** Additional PRN Sequences. Among all unique L5-code sequences that could be generated using different initial states as described in Section 3.2.1.1, 126 sequences (63 I5 and 63 Q5) are selected and assigned in Table 3-Ia and Table 3-Ib. An additional 294 sequences (147 I5 and 147 Q5) are selected and assigned with PRN numbers in the below Table 6-II. Any assignment of an L5 PRN number and its code sequence for any additional SV and/or other L5

signal applications, such as Satellite Based Augmentation System (SBAS) satellite signals, will be selected from the sequences of Table 6-II.

Table 6-II. Additional Code Phase Assignments (sheet 1 of 5)					
PRN	XB Code Adv	ance – Chips**	Initial XB (	Code State***	
Signal No.	I5	Q5	I5	Q5	
64	7789	5246	1000100010001	1001101001111	
65	2311	4259	0001000101111	0001100100010	
66	7432	5907	0001100111111	0000111111000	
67	5155	3870	1010101100001	0011100100111	
68	1593	3262	0101011111001	0000001010010	
69	5841	7387	0101101100001	1100111111001	
70	5014	3069	1000101111011	0111111110010	
71	1545	2999	0111011001111	0101011111111	
72	3016	7993	0001011011000	1100001111011	
73	4875	7849	1110000111000	1110100110101	
74	2119	4157	0111010010001	1010010110101	
75	229	5031	0001101111000	0101111101111	
76	7634	5986	1111001010100	1010110110010	
77	1406	4833	1011101110100	1101110110001	
78	4506	5739	0000100110000	1010000100100	
79	1819	7846	1100010000111	0100110101010	
80	7580	898	0001101111111	1000011100011	
81	5446	2022	1100110101101	1100111011010	
82	6053	7446	1101011001011	0010110001111	
83	7958	6404	1100001101100	1101101110110	
84	5267	155	1011110110001	1101111001001	
85	2956	7862	0111010110101	1100100000000	
86	3544	7795	1100101101101	1001101000100	
87	1277	6121	1100111011111	1111011010001	
88	2996	4840	1011111111011	0110101110111	
89	1758	6585	1110100100111	0000100111111	
90	3360	429	1111110010100	1101101001110	
91	2718	6020	0101001111110	1100111001011	
92	3754	200	0010100100101	1010111000011	
93	7440	1664	0001111000011	1110110010110	
94	2781	1499	1100111000000	1110100011111	
95	6756	7298	1110010101000	0001101100011	
96	7314	1305	0111000101001	0001011010110	
97	208	7323	1111101010101	0000001000111	
98	5252	7544	1010111001101	1010011000000	
99	696	4438	1100101001011	1000111101101	

<sup>\*\*</sup> XB Code Advance is the number of XB clock cycles beyond an initial state of all 1s.

<sup>\*\*\*</sup> In the binary notation for the first 13 chips of the I5 and Q5 XB codes as shown in these columns. The rightmost bit is the first bit out. Since the initial state of the XA Code is all 1s, these first 13 chips are also the complement of the initial states of the I5 or Q5-codes.

Table 6-II. Additional Code Phase Assignments (sheet 2 of 5)					
PRN	XB Code Adv	vance – Chips**	Initial XB Code State***		
Signal No.	I5	Q5	I5	Q5	
100	527	2485	0010100000110	1101101011100	
101	1399	3387	1101000010001	1000010110011	
102	5879	7319	0111011010011	0010001110001	
103	6868	1853	1101110101111	0010100100110	
104	217	5781	0111011011111	0100000111111	
105	7681	1874	1010101001100	1000001111101	
106	3788	7555	1011010000011	1010101111010	
107	1337	2132	0101100000000	1111010101010	
108	2424	6441	0000111101000	11010101111100	
109	4243	6722	0110000111011	1111100001010	
110	5686	1192	1101100100000	1111000010001	
111	1955	2588	0011011101111	1101111011101	
112	4791	2188	1001111101100	0010000100001	
113	492	297	0100011000110	1100100111100	
114	1518	1540	0111000101110	1100111100011	
115	6566	4138	0100010110000	1001100001111	
116	5349	5231	0110111100100	1110011001001	
117	506	4789	0001110010010	0111110110011	
118	113	659	1110110110101	1111011010110	
119	1953	871	1101110111100	1000111011110	
120	2797	6837	1101001100010	1101001011001	
121	934	1393	1100011001100	0010001111001	
122	3023	7383	1000011000101	1111110011111	
123	3632	611	1111011011011	1000110000001	
124	1330	4920	0000001100100	0000111100011	
125	4909	5416	1101110000101	0111011011100	
126	4867	1611	1100001000010	0101101010100	
127	1183	2474	0001101001101	0000101010111	
128	3990	118	1010100101011	1010111101101	
129	6217	1382	1111011110100	0100010000010	

<sup>\*\*</sup> XB Code Advance is the number of XB clock cycles beyond an initial state of all 1s.

32

<sup>\*\*\*</sup> In the binary notation for the first 13 chips of the I5 and Q5 XB codes as shown in these columns. The rightmost bit is the first bit out. Since the initial state of the XA Code is all 1s, these first 13 chips are also the complement of the initial states of the I5 or Q5-codes.

Table 6-II. Additional Code Phase Assignments (sheet 3 of 5)					
PRN	XB Code Adv	ance – Chips**	Initial XB (	Code State***	
Signal No.	I5	Q5	I5	Q5	
130	1224	1092	11111111101100	1010111011111	
131	1733	7950	0000010000111	0110001000010	
132	2319	7223	1111110000010	1011000011010	
133	3928	1769	0011100111011	1000100000111	
134	2380	4721	1101100010101	1001011110110	
135	841	1252	0101011111011	1000001011000	
136	5049	5147	0001100011011	0000110010111	
137	7027	2165	0001101110111	0010101101011	
138	1197	7897	1110011110000	0011100001100	
139	7208	4054	0111100011111	0100011001011	
140	8000	3498	0011101110000	1010101001111	
141	152	6571	1111001001000	0100001000101	
142	6762	2858	0001101110010	0000001111100	
143	3745	8126	0101100111100	1101001110111	
144	4723	7017	0010010111101	11101111110001	
145	5502	1901	1101110110011	1110111010001	
146	4796	181	0011110011111	0001010110011	
147	123	1114	1001010101111	0111111000101	
148	8142	5195	0111111101111	0100010011100	
149	5091	7479	0000100100001	1110000010011	
150	7875	4186	1110001101011	0110010101000	
151	330	3904	1111010010001	0000100000100	
152	5272	7128	1011010111101	0100100101011	
153	4912	1396	0001101110000	1000010001111	
154	374	4513	0000010111100	1110101000010	
155	2045	5967	0100101111100	1110000111011	
156	6616	2580	1110110111010	1110110010010	
157	6321	2575	1101110101011	1001001001000	
158	7605	7961	1101000110001	0011100001101	
159	2570	2598	0100100010100	0000111101110	

<sup>\*\*</sup> XB Code Advance is the number of XB clock cycles beyond an initial state of all 1s.

<sup>\*\*\*</sup> In the binary notation for the first 13 chips of the I5 and Q5 XB codes as shown in these columns. The rightmost bit is the first bit out. Since the initial state of the XA Code is all 1s, these first 13 chips are also the complement of the initial states of the I5 or Q5-codes.

Table 6-II. Additional Code Phase Assignments (sheet 4 of 5)					
PRN	XB Code Adv	vance – Chips**	Initial XB (	Code State***	
Signal No.	I5	Q5	I5	Q5	
160	2419	4508	1110100011001	0100001001100	
161	1234	2090	1101000100111	0010111011110	
162	1922	3685	0101101110111	0110011011010	
163	4317	7748	0010111010000	1101011000010	
164	5110	684	0000111011000	1100010001101	
165	825	913	1001110111011	1010111011001	
166	958	5558	0110100011111	0100001001010	
167	1089	2894	0111011111100	0111000111010	
168	7813	5858	1010010011010	0000000110000	
169	6058	6432	0010011010110	11001011111100	
170	7703	3813	0111100110011	0001100100111	
171	6702	3573	0000011011011	0011010111001	
172	1714	7523	1001010011010	0001000011100	
173	6371	5280	11010101011111	1100101010110	
174	2281	3376	1110111001010	1101110010010	
175	1986	7424	0010011110110	1111111111001	
176	6282	2918	0011110101001	0110000001010	
177	3201	5793	1111010000111	0100101001010	
178	3760	1747	0010010010100	1111110100100	
179	1056	7079	0100101110010	1100010101011	
180	6233	2921	1101110110000	1100110000001	
181	1150	2490	1000111111011	0111111011010	
182	2823	4119	0101101110000	0111000011101	
183	6250	3373	0001110101011	1110010010110	
184	645	977	1111000100010	0011111111000	
185	2401	681	0101001000011	0010001101101	
186	1639	4273	00111011111100	0001100110011	
187	2946	5419	10110101111010	0100111011011	
188	7091	5626	0000001010011	0110111000101	
189	923	1266	0010011111101	1101011100011	

<sup>\*\*</sup> XB Code Advance is the number of XB clock cycles beyond an initial state of all 1s.

<sup>\*\*\*</sup> In the binary notation for the first 13 chips of the I5 and Q5 XB codes as shown in these columns. The rightmost bit is the first bit out. Since the initial state of the XA Code is all 1s, these first 13 chips are also the complement of the initial states of the I5 or Q5-codes.

Table 6-II. Additional Code Phase Assignments (sheet 5 of 5)					
PRN	XB Code Adv	ance – Chips**	Initial XB Code State***		
Signal No.	I5	Q5	I5	Q5	
190	7045	5804	1111100011000	1001110110001	
191	6493	2414	1101101101100	0001100110110	
192	1706	6444	1101010010110	1101101010111	
193	5836	4757	0110000101110	1001110000111	
194	926	427	0110010011111	0110100111010	
195	6086	5452	1000111001100	0110001100110	
196	950	5182	1111101110001	0000100001100	
197	5905	6606	00111111100001	0101000101101	
198	3240	6531	0000001110001	1000001010111	
199	6675	4268	1010110100100	0011001110001	
200	3197	3115	0100001110110	0100011100110	
201	1555	6835	0111110100011	0100101100101	
202	3589	862	0001111001011	1110001010111	
203	4555	4856	1010100011011	1010110110100	
204	5671	2765	1001101110011	1111101101000	
205	6948	37	0010111000001	1000001110100	
206	4664	1943	1101100001111	1000010101100	
207	2086	7977	11101111101001	1100001001101	
208	5950	2512	0110110101101	1111111000011	
209	5521	4451	0111110110010	0001011110011	
210	1515	4071	1000101110111	1001000100001	

<sup>\*\*</sup> XB Code Advance is the number of XB clock cycles beyond an initial state of all 1s.

# 6.4 Operational Protocols.

### **6.4.1** Lower PRN Numbers Versus Upper PRN Numbers. See IS-GPS-200.

- **6.4.2 PRN Number Consistency.** For a given satellite, the same PRN number will be assigned to all operational signals (signals modulated by standard PRN code with data that indicates the signal health is OK).
- **6.4.3 PRNs 33 and 37.** See IS-GPS-200.
- **6.4.4 PRNs 33 through 63.** See IS-GPS-200.

<sup>\*\*\*</sup> In the binary notation for the first 13 chips of the I5 and Q5 XB codes as shown in these columns. The rightmost bit is the first bit out. Since the initial state of the XA Code is all 1s, these first 13 chips are also the complement of the initial states of the I5 or Q5-codes.

### 10 APPENDIX I. LETTERS OF EXCEPTION.

- **10.1** <u>Scope.</u> Approval of this document, as well as approval of any subsequent changes to the document, can be contingent upon a "letter of exception." This appendix depicts such "letters of exception" when authorized by the GPS Directorate.
- **10.2** <u>Applicable Documents.</u> The documents listed in Section 2.0 shall be applicable to this appendix.
- **10.3** <u>Letters of Exception.</u> Any letter of exception which is in force for the revision of the IS is depicted in Figure 10.3-1, 10.3-2, 10.3-3, and 10.3-4.

The Boding Company 5304 Bossa Avenus Humington Beach, CA 92847

December 6, 2004 AFSS-GPSHF-K211-JMH-04-0717

Headquarters, Space and Missile (SMC) SMC/GPK 2420 Vela Way, Suite 1467 El Segundo, CA 90245-4659



Dear Ms. Brown:

F04701-96-C-0025; Global Positioning System (GPS) Block HY-Disposition of IRN-705-001 Subject:

 (a) Email from S. Coletti/Booing to Folicia Brown and Lt. Kevin Reyes/AF on November 22, 2004
 (b) PCOL 04-085 letter dated November 02, 2004 Reference:

Per the Referenced (a) omail, Booling provided its assessment of both cost and schedule impact to the latest IRN version (November 11, 2004). Boeing has reviewed the IRN-705-001 per the Referenced (b) letter, Please note that our review was based upon the receipt of the IRN versus the PIRN. The content of this document that has been determined out of scope of the Boeing contractual baseline

Booing has reviewed IRN-705-001 per the original direction of the Referenced (b) tetter. The content of this document that has been determined out of scope of the Booing contractual baseline is listed below:

#### IRN-705-001

Location	Exception	Rationale for Exception	Cost	Schedule (mpact
20.3.3 Page 44	New L5 CNAV	L5 CNAV Message 31 requires change to UG, Pred, UCD and possible generation of raw data.	ligh	Iligh
20.3.3 Page 45	New L5 CNAV Messages	L5 CNAV Message 32 requires change to UG, Pred, UCD and possible generation of raw data.	High	High
20.3.3 Page 47	New L5 CNAV Messages	1.5 CNAV Message 34 requires change to UG, Prod, UCD and possible generation of raw data.	Hīgī	High

Figure 10.3-1. Letters of Exception

Yho Boolog Company 6301 Boles Avonus Huntington Boach, CA 92847

ARSS-GPSIIF-K211-JMH-04-0717 Headquarters, Space and Missile (SMC) Page 2 of 2



20.3.3	New L5	L5 CNAV Message 35 requires	High	High
Page 48	CNAV	change to UG, Pred, UCD and	-	-
_	Messages	possible generation of raw data.		
20.3.3	New L5	LS CNAV Message 36 requires	High	High
Page 49	CNAV	change to UG, Pred, UCD and	-	-
_	Messages	possible generation of raw data.		
20.3.3	New LS	L5 CNAV Message 37 requires	High	Hügh
Page 50	CNAV	change to UG, Pred, UCD and	_	-
	Mcssages	possible generation of raw data.		
20.3.3	New L5	L5 CNAV Message 13 requires	High	High
Page 52	CNAV	change to UG, Pred, UCD and	_	-
	Measages	possible generation of raw data.		
20.3.3	New L5	L5 CNAV Message 14 requires	High	High
Page 53	CNAV	change to UG, Pred, UCD and	_	
	Messages	possible generation of raw data.		
20.3.3	New L5	L5 CNAV Message 15 requires	High	High
Page 54	CNAV	change to UG, Pred, UCD and	•	•
•	Мексадов	possible generation of raw data.	l	1

For purposes of this assessment, a High Impact to cost is defined as greater than  $\$250,\!000$ .

Should you require any additional information please contact the undersigned at telephone  $(714)\ 896-2561$ .

M. Plognes
F. M. Plognes
Sr. Manager - Contracts & Pricing
GPS IIP Program
Air Force Space Systems
M/C: H011-B145

JMH:jmh

Figure 10.3-2. Letters of Exception (continued).

The Boeing Company 2201 Seal Beach Blvd Seal Beach, CA 90740-1515

NCS-GPSIIF-3100-SCP-10-0139 June 8, 2010

United States Air Force Headquarters Global Positioning Wing (AFSPC) Los Angeles Air Force Base ATTN: Ms. Allison Flanagan, PCO GPSW/GPK 483 N. Aviation Boulevard El Segundo, CA 90245-2808

Subject:

Contract F04701-96-C-0025; Global Positioning System (GPS) Block IIF, ADP

152, Letter of Exception to IS-GPS-705A, dated 23 November 2009

Ref

PCOL 10-045 dated 27 May 2010, Request for Impact Assessment on IS-

GPS-705A Changes

Dear Ms. Flanagan:

The IS-GPS-705A ICD defines the interface between the NAVSTAR GPS Space Segment and the NAV User Segment for L5 signals. The Boeing Company has reviewed and takes Exception to the following paragraphs of IS-GPS-705A, dated 23 November 2009.

- Section 3.3.1.7.2 Group Delay Differential: including consideration of temperature and antenna effects impacts IIF SV requirement
- Section 3.3.1.8 Signal Coherence: expanded scope of requirement (variable time difference) would require additional testing/verification

Should you require any additional information, please contact Mr. Steve Colletti at (562) 797-1333 or the undersigned.

Sincerely,

Stoth Argendl For

Contract Management GPS Programs

sonja.c.peltz@boeing.com (562) 797-1048

(302) /3/-104

Attachments; none

cc: Ms. Rei Okabayashi, ACO

Ms. Tracy Malone Capt. Ryan Findley Capt. Patrick Jackson

Capt. Neal Roach Mr. Vimal Gopal DCMA/H014-A407 SE&I/EN CM/DM GPSW/GP2S

GPSW/GP2S GPSW/ENR SE&I/EN

Figure 10.3-3. Letters of Exception (continued)

The Boeing Company 2201 Seal Beach Blvd. Seal Beach, CA 90740-1515

June 28, 2010 NCS-GPSIIF-3100-SCP-10-0172

United States Air Force Headquarters Global Positioning Wing (AFSPC) Los Angeles Air Force Base ATTN: Ms. Allison Flanagan, PCO GPSW/GPK 483 N. Aviation Boulevard El Segundo, CA 90245-2808

Subject:

Contract F04701-96-C-0025; Global Positioning System (GPS) Block IIF, ADP 152,

Letter of Exception to IS-GPS-200E, dated 28 January 2010

Ref:

PCOL 10-023 dated 19 March 2010, Request for Impact Assessment on IS-GPS-200E

Changes

Dear Ms. Flanagan:

The Boeing Company has reviewed IS-GPS-200E, dated 28 January 2010, for cost and schedule impacts. Boeing approves IS-GPS-200E, dated 28 January 2010 with the following Exceptions. If these exceptions are accepted, there is no cost or schedule impact.

- Section 3.3.1.2 Correlation Loss: expanded scope of requirement (variable time difference) would require additional testing/verification
- Section 3.3.1.8 Signal Coherence: revised wording of requirement would require additional analysis/verification
- Section 3.3.1.5.1 Phase Quadrature: expanded scope of requirement (+/-100 miliradians) would require additional testing/verification. Additionally, Bit 273 (Integrity Status Flag) change levies a CS requirement.
- Section 3.3.1.7.2 Group Delay Differential: including consideration of temperature and antenna effects impacts IIF SV requirement
- Section 20.3.3.3.1.3 SV Accuracy: expanded scope of requirement (URA Integrity Properties) is out of scope to the existing IIF SV Contract
- Globally, all references to Integrity Status Flag (ISF) and Bit 273 are new requirements being levied on the CS

Should you require any additional information, please contact Mr. Steve Colletti at (562) 797-1333 or the undersigned.

Sincerely,

Sonja Peltz Contract Management GPS Programs

sonja.c.peltz@boeing.com

(562) 797-1048

Attachments: none

cc: Ms. Rei Okabayashi, ACODCMA/H014-A407

Ms. Tracy Malone SE&I/EN CM/DM
Capt. Ryan Findley GPSW/GP2S
Capt. Patrick Jackson GPSW/GP2S
Capt. Neal Roach GPSW/ENR
Mr. Vimal Gopal SE&I/EN

Figure 10.3-4. Letters of Exception (continued)

# 20 APPENDIX II. GPS NAVIGATION DATA STRUCTURE FOR L5 CNAV DATA, $D_5(t)$

**20.1** Scope. This appendix describes the specific GPS L5 civil navigation (CNAV) data structure denoted by,  $D_5(t)$ .

### **20.2 Applicable Documents.**

Specifications

**20.2.1** Government Documents. In addition to the documents listed in paragraph 2.1, the following documents of the issue specified contribute to the definition of the CNAV data related interfaces and form a part of this Appendix to the extent specified herein.

<u>specifications</u>
None
<u>Standards</u>
None
Other Publications
None

**20.2.2 Non-Government Documents.** In addition to the documents listed in paragraph 2.2, the following documents of the issue specified contribute to the definition of the CNAV data related interfaces and form a part of this Appendix to the extent specified herein.

Specifications
None

Other Publications

None

## 20.3 Requirements.

- **20.3.1** <u>Data Characteristics.</u> The L5 channel data stream mostly contains the same data as the L2 C channel. The data stream shall be transmitted by the SV on the L5 channel at the rate of 50 bps with rate 1/2 FEC resulting in 100 sps.
- **20.3.2** <u>Message Structure.</u> As shown in Figures 20-1 through 20-14, the L5 CNAV message structure utilizes a basic format of six-second 300-bit long messages. Each message contains a

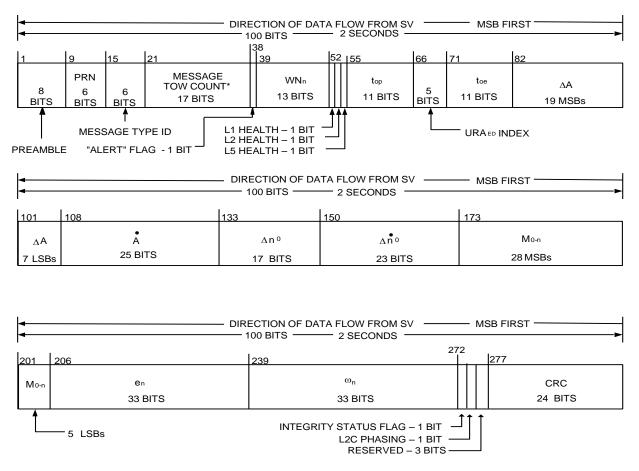
Cyclic Redundancy Check (CRC) parity block consisting of 24 bits covering the entire six-second message (300 bits) (reference Section 20.3.5).

Message type 0 (zero) is defined to be the default message. In the event of message generation failure, the SV shall replace each affected message type with the default message type. In the event that a particular message is not assigned (by the CS) a particular message type for broadcast, the SV shall generate and broadcast the default message type in that message slot.

Currently undefined and unused message types are reserved for future use.

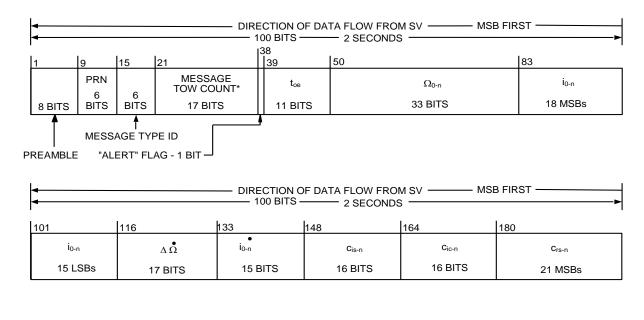
Block IIF SVs have the capability of storing at least 48 hours of CNAV navigation data, with current memory margins, to provide CNAV positioning service without contact from the CS for that period. GPS III SVs have the capability of providing up to 60 days of CNAV positioning service without contact from the CS. The timeframe is defined by the CS.

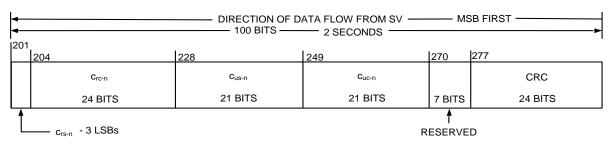
**20.3.3** Message Content. Each message starts with an 8-bit preamble - 10001011, followed by a 6-bit PRN number of the transmitting SV, a 6-bit message type ID with a range of 0 (000000) to 63 (111111), and the 17-bit message time of week (TOW) count. When the value of the message TOW count is multiplied by 6, it represents SV time in seconds at the start of the next 6-second message. An "alert" flag, when raised (bit 38 = "1"), indicates to the user that the signal URA components may be worse than indicated in the associated message types and that he shall use at his own risk. For each default message (Message Type 0), bits 39 through 276 shall be alternating ones and zeros and the message shall contain a proper CRC parity block.



<sup>\*</sup> MESSAGE TOW COUNT = 17 MSB OF ACTUAL TOW COUNT AT START OF NEXT 6 SECOND MESSAGE

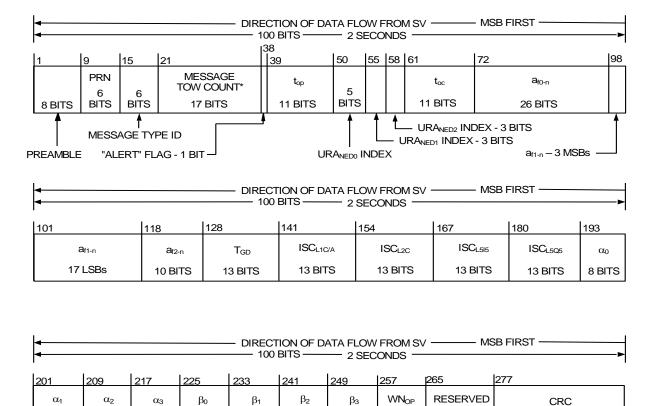
Figure 20-1. Message type 10 - Ephemeris 1





<sup>\*</sup> MESSAGE TOW COUNT = 17 MSB OF ACTUAL TOW COUNT AT START OF NEXT 6-SECOND MESSAGE

Figure 20-2. Message type 11 - Ephemeris 2



8 BITS

8 BITS

8 BITs

8 BITS

8 BITS

8 BITS

Figure 20-3. Message type 30 - Clock, IONO & Group Delay

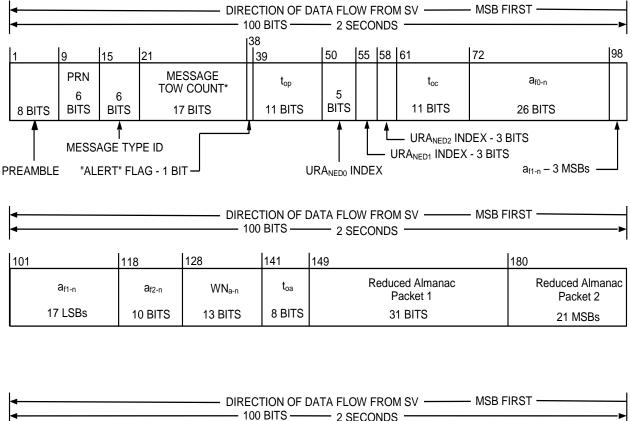
8 BITS

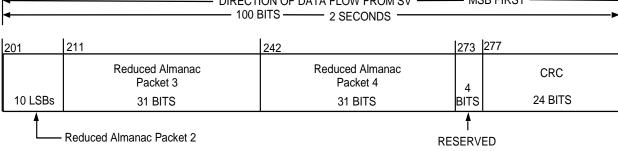
8 BITS

12 BITS

24 BITS

<sup>\*</sup> MESSAGE TOW COUNT = 17 MSB OF ACTUAL TOW COUNT AT START OF NEXT 6-SECOND MESSAGE





<sup>\*</sup> MESSAGE TOW COUNT = 17 MSB OF ACTUAL TOW COUNT AT START OF NEXT 6-SECOND MESSAGE

46

Figure 20-4. Message type 31 - Clock & Reduced Almanac

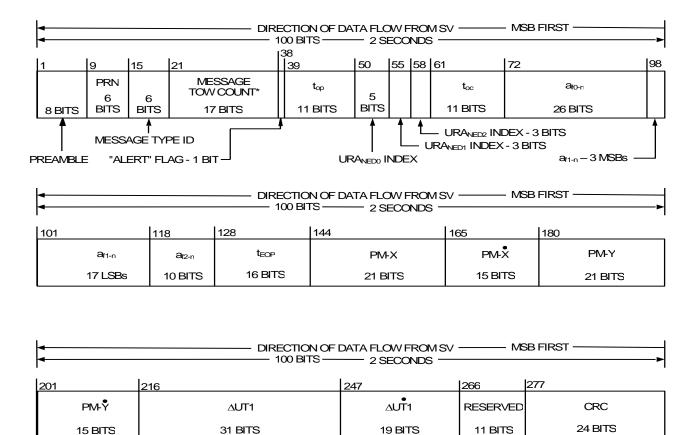
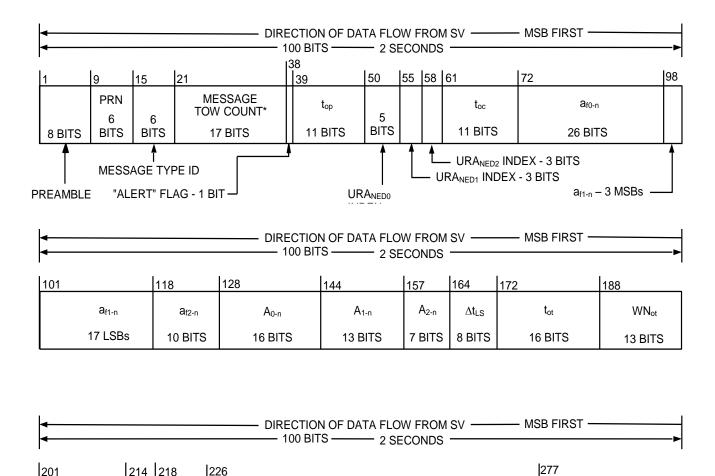


Figure 20-5. Message type 32 - Clock & EOP

<sup>\*</sup> MESSAGE TOW COUNT = 17 MSB OF ACTUAL TOW COUNT AT START OF NEXT 6-SECOND MESSAGE



DN

4

BITS

 $\Delta t_{\text{LSF}}$ 

8 BITS

 $WN_{\mathsf{LSF}}$ 

13 BITS

Figure 20-6. Message type 33 - Clock & UTC

48

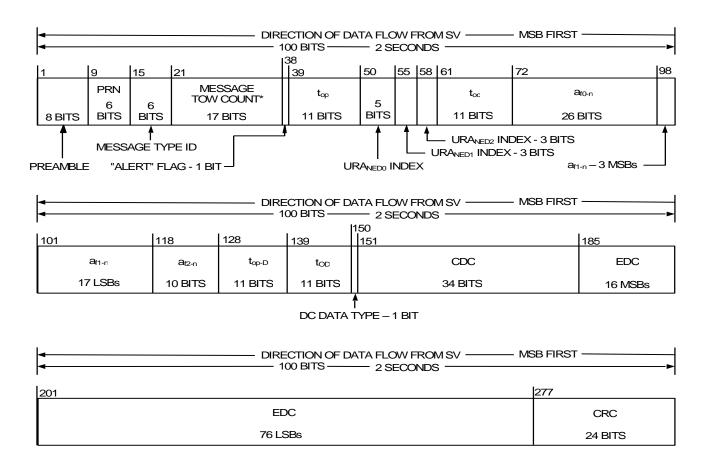
**RESERVED** 

51 BITS

**CRC** 

24 BITS

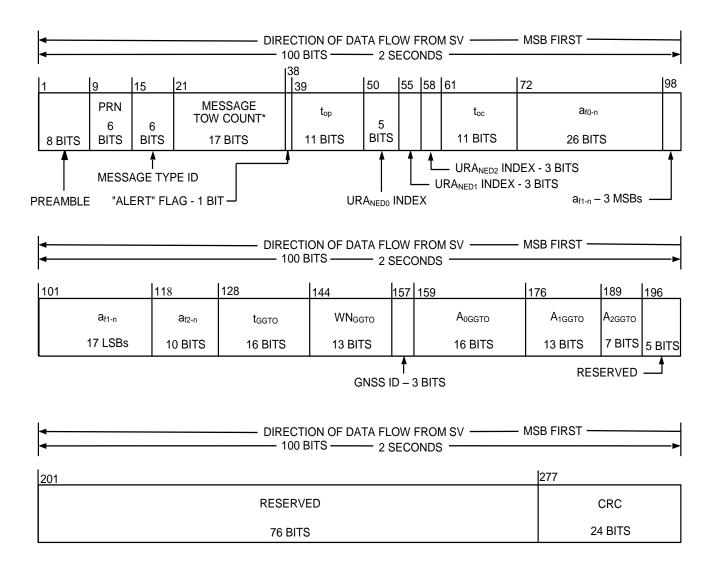
<sup>\*</sup> MESSAGE TOW COUNT = 17 MSB OF ACTUAL TOW COUNT AT START OF NEXT 6-SECOND MESSAGE



MESSAGE TOW COUNT = 17 MSB OF ACTUAL TOW COUNT AT START OF NEXT 6-SECOND MESSAGE

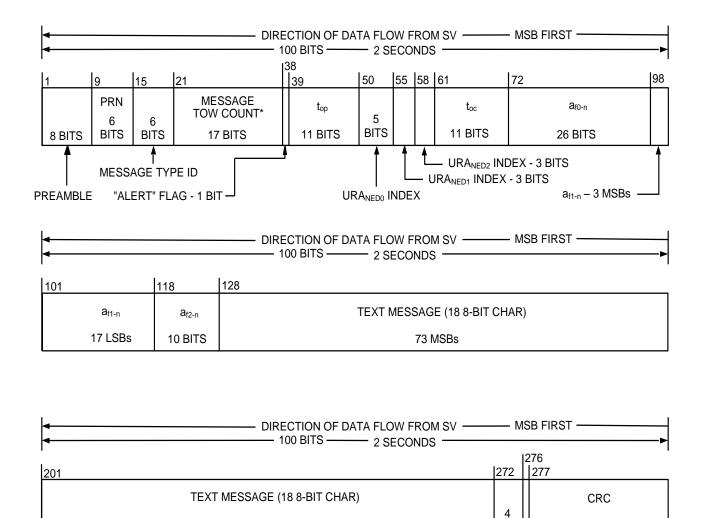
CDC = Clock Differential Correction EDC = Ephemeris Differential Correction

Figure 20-7. Message type 34 - Clock & Differential Correction



<sup>\*</sup> MESSAGE TOW COUNT = 17 MSB OF ACTUAL TOW COUNT AT START OF NEXT 6-SECOND MESSAGE

Figure 20-8. Message type 35 - Clock & GGTO



71 LSBs

Figure 20-9. Message type 36 - Clock & Text

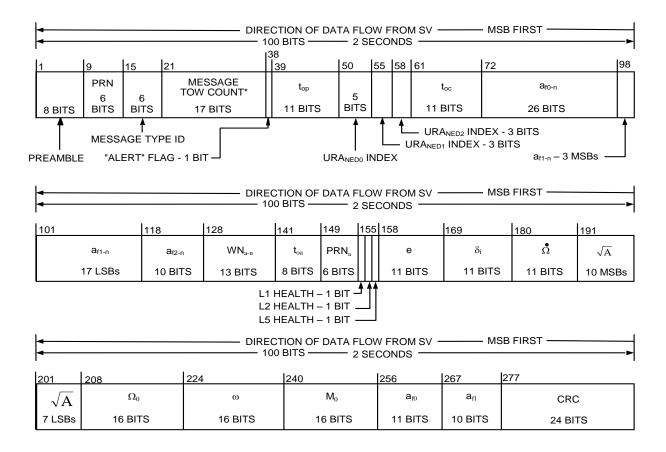
24 BITS

RESERVED - 1 BIT

lвıтs

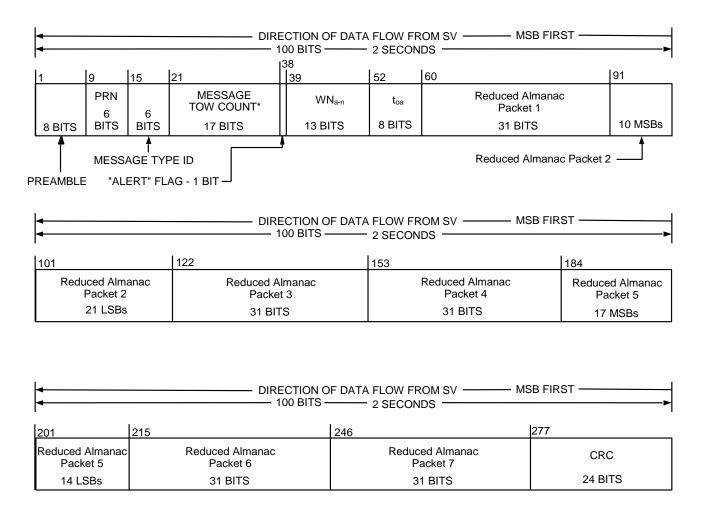
TEXT PAGE -

<sup>\*</sup> MESSAGE TOW COUNT = 17 MSBs OF ACTUAL TOW COUNT AT START OF NEXT 6-SECOND MESSAGE



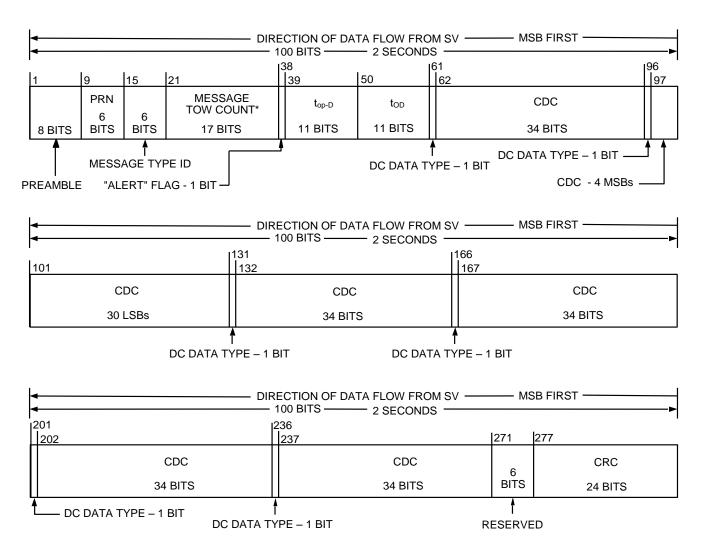
<sup>\*</sup> MESSAGE TOW COUNT = 17 MSBs OF ACTUAL TOW COUNT AT START OF NEXT 6-SECOND MESSAGE

Figure 20-10. Message Type 37 - Clock & Midi Almanac



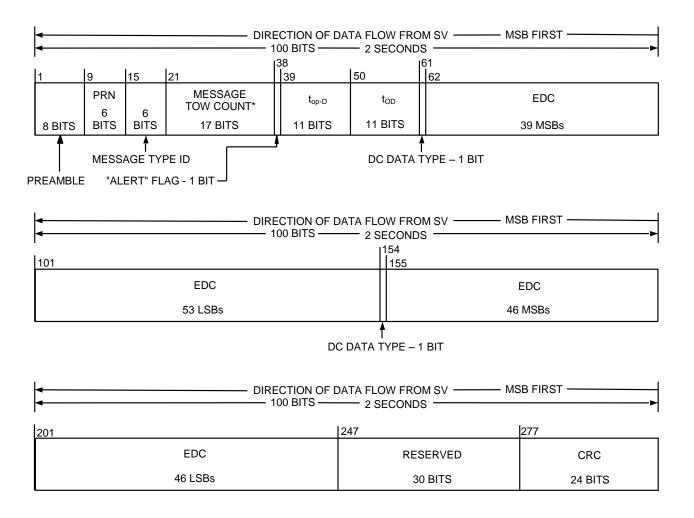
<sup>\*</sup> MESSAGE TOW COUNT = 17 MSBs OF ACTUAL TOW COUNT AT START OF NEXT 6-SECOND MESSAGE

Figure 20-11. Message type 12 - Reduced Almanac



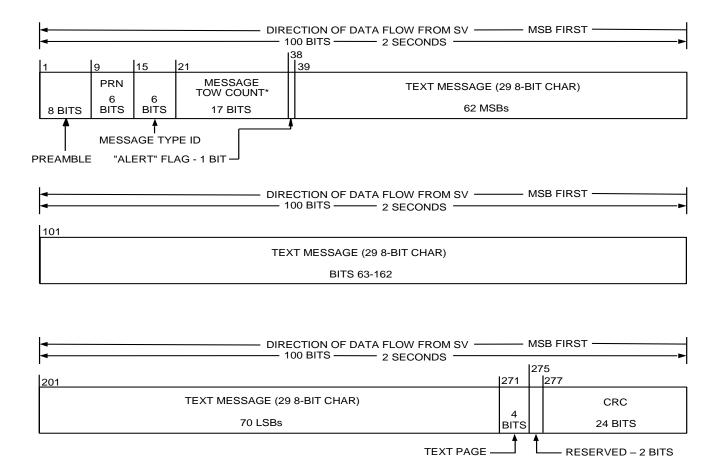
<sup>\*</sup> MESSAGE TOW COUNT = 17 MSBs OF ACTUAL TOW COUNT AT START OF NEXT 6-SECOND MESSAGE CDC = Clock Differential Correction

Figure 20-12. Message type 13 - Clock Differential Correction



<sup>\*</sup> MESSAGE TOW COUNT = 17 MSBs OF ACTUAL TOW COUNT AT START OF NEXT 6-SECOND MESSAGE EDC = Ephemeris Differential Correction

Figure 20-13. Message type 14 - Ephemeris Differential Correction



<sup>\*</sup> MESSAGE TOW COUNT = 17 MSB OF ACTUAL TOW COUNT AT START OF NEXT 6-SECOND MESSAGE

Figure 20-14. Message type 15 - Text

### 20.3.3.1 Message Types 10 and 11 Ephemeris and Health Parameters.

**20.3.3.1.1** Message Types 10 and 11 Ephemeris and Health Parameter Content. The contents of the SV health, ephemeris representation and accuracy parameters in message types 10 and 11 are defined below, followed by material pertinent to the use of the data. Message type 10, in conjunction with message type 11, provides users with the requisite data to calculate SV position. The general format of message types 10 and 11 consists of data fields for reference time tags, a set of gravitational harmonic correction terms, rates and rate corrections to quasi-Keplerian elements, and an accuracy indicator for ephemeris-related data.

The broadcast group delay differential correction terms apply to the pseudorange measurements produced by an ideal correlation receiver with a bandwidth of 20.46 MHz centered at the reference waveform nominal frequency whose phase is linear over that bandwidth using an exact replica of the reference waveform in an early-late discriminator having a correlator spacing of

97.75 nanoseconds. The group delay differential correction terms may not apply to pseudorange measurements produced by different methods due to potential distortion of the transmitted waveform. Users employing pseudorange measurement methods different from the defined method must account for the potential inapplicability of the group delay differential correction terms.

The  $t_{oe}$  term shall provide the user with a convenient means for detecting any change in the ephemeris representation parameters. The  $t_{oe}$  is provided in both message type 10 and 11 for the purpose of comparison with the  $t_{oc}$  term in message type 30 - 37. Whenever these three terms do not match, a data set cutover has occurred and new data must be collected. The timing of the  $t_{oe}$  and constraints on the  $t_{oe}$  are defined in paragraph 20.3.4.4.

Any change in the message type 10 and 11 ephemeris data will be accomplished with a simultaneous change in the  $t_{oe}$  value. The CS will assure the  $t_{oe}$  value for Block IIR-M/IIF and SS will assure the  $t_{oe}$  value for GPS III, for at least the first data set transmitted by an SV after an upload, is different from that transmitted prior to the cutover. See Section 20.3.4.5 for additional information regarding  $t_{oe}$ .

The CNAV messages contain information that allows users to take advantage of situations when integrity is assured to the enhanced level. This is accomplished using a composite integrity assured URA value in conjunction with an integrity status flag. The composite integrity assured URA (IAURA) value is the RSS of an elevation-dependent function of the upper bound value of the URA $_{\text{NED}}$  component and the upper bound value of the URA $_{\text{NED}}$  component. The composite IAURA value is assured to the enhanced level only when the integrity status flag is "1"; otherwise the IAURA value is assured to the legacy level.

Bit 272 of Message Type 10 is the Integrity Status Flag (ISF). A "0" in bit position 272 indicates that the conveying signal is provided with the legacy level of integrity assurance. That is, the probability that the instantaneous URE of the conveying signal exceeds 4.42 times the current broadcast IAURA value, for more than 5.2 seconds, without an accompanying alert, is less than 1E-5 per hour.

A "1" in bit-position 272 indicates that the conveying signal is provided with an enhanced level of integrity assurance. That is, the probability that the instantaneous URE of the conveying signal exceeds 5.73 times the current broadcast IAURA value, for more than 5.2 seconds, without an accompanying alert, is less than 1E-8 per hour. The probabilities associated with the nominal and lower bound values of the current broadcast  $URA_{ED}$  index,  $URA_{NED}$  indexes, and related URA values are not defined.

In this context, an "alert" is defined as any indication or characteristic of the conveying signal, as specified elsewhere in this document, which signifies to users that the conveying signal may be invalid or should not be used, such as the health bits not indicating operational-healthy, broadcasting non-standard code parity error, etc.

Bit 273 of Message Type 10 indicates the phase relationship between L2C and P(Y) as specified in section 3.3.1.5.1 of IS-GPS-200.

**20.3.3.1.1.1** <u>Transmission Week Number.</u> Bits 39 through 51 of message type 10 shall contain 13 bits which are a modulo-8192 binary representation of the current GPS week number at the start of the data set transmission interval (see paragraph 6.2.4 of IS-GPS-200).

**20.3.3.1.1.2** Signal Health (L1/L2/L5). The three, one-bit, health indication in bits 52 through 54 of message type 10 refers to the L1, L2, and L5 signals of the transmitting SV. The health of each signal is indicated by,

0 = Signal OK,

1 = Signal bad or unavailable.

The predicted health data will be updated at the time of upload when a new data set has been built by the CS. The transmitted health data may not correspond to the actual health of the transmitting SV.

Additional SV health data are given in the almanac in message types 12, 31, and 37. The data given in message type 10 may differ from that shown in the other messages of the transmitting SV and/or other SVs since the latter may be updated at a different time.

**20.3.3.1.1.3** <u>Data Predict Time of Week.</u> Bits 55 through 65 of message type 10 shall contain the data predict time of week  $(t_{op})$ . The top term provides the epoch time of week of the state estimate utilized for the prediction of satellite quasi-Keplerian ephemeris parameters.

**20.3.3.1.1.4** Elevation-Dependent (ED) Accuracy. Bits 66 through 70 of message type 10 shall contain the elevation-dependent (ED) component User Range Accuracy (URA<sub>ED</sub>) index for the standard positioning service user. The URA<sub>ED</sub> index shall provide the ED-related URA index for the current ephemeris curve fit interval. While the ED-related URA may vary over the ephemeris curve fit interval and over the satellite footprint, the URA<sub>ED</sub> index (N) in message type 10 shall correspond to the maximum URA<sub>ED</sub> expected over the entire ephemeris curve fit interval for the worst-case location within the SV footprint (i.e., nominally two points at the edge of the SV footprint). At the best-case location within the SV footprint (i.e., nominally directly below the SV along the SV nadir vector), the corresponding URA<sub>ED</sub> is zero.

The URA<sub>ED</sub> index is a signed, two's complement integer in the range of +15 to -16 and has the following relationship to the ED URA:

<u>URA<sub>ED</sub> Index</u>		<u>URA<sub>ED</sub> (meters)</u>	
15	6144.00	$<$ URA $_{\rm ED}$	(or no accuracy prediction is available)
14	3072.00	$<$ URA <sub>ED</sub> $\leq$	6144.00
13	1536.00	$<$ URA <sub>ED</sub> $\leq$	3072.00
12	768.00	$<$ URA <sub>ED</sub> $\leq$	1536.00
11	384.00	$<$ URA <sub>ED</sub> $\leq$	768.00
10	192.00	$<$ URA <sub>ED</sub> $\leq$	384.00
9	96.00	$<$ URA <sub>ED</sub> $\leq$	192.00
8	48.00	$<$ URA <sub>ED</sub> $\leq$	96.00
7	24.00	$<$ URA <sub>ED</sub> $\leq$	48.00
6	13.65	$<$ URA <sub>ED</sub> $\leq$	24.00
5	9.65	$<$ URA <sub>ED</sub> $\leq$	13.65
4	6.85	$<$ URA <sub>ED</sub> $\leq$	9.65
3	4.85	$<$ URA <sub>ED</sub> $\leq$	6.85
2	3.40	$<$ URA <sub>ED</sub> $\leq$	4.85
1	2.40	$<$ URA <sub>ED</sub> $\leq$	3.40
0	1.70	$<$ URA <sub>ED</sub> $\leq$	2.40
-1	1.20	$<$ URA <sub>ED</sub> $\leq$	1.70
-2	0.85	$<$ URA <sub>ED</sub> $\leq$	1.20
-3	0.60	$<$ URA <sub>ED</sub> $\leq$	0.85
-4	0.43	$<$ URA <sub>ED</sub> $\leq$	0.60
-5	0.30	$<$ URA <sub>ED</sub> $\leq$	0.43
-6	0.21	$<$ URA <sub>ED</sub> $\leq$	0.30
-7	0.15	$<$ URA <sub>ED</sub> $\leq$	0.21
-8	0.11	$<$ URA <sub>ED</sub> $\leq$	0.15

-9	0.08	$<$ URA $_{\rm ED}$	$\leq$	0.11
-10	0.06	< URA <sub>ED</sub>	<u>≤</u>	0.08
-11	0.04	< URA <sub>ED</sub>	<u>≤</u>	0.06
-12	0.03	< URA <sub>ED</sub>	$\leq$	0.04
-13	0.02	< URA <sub>ED</sub>	<u>≤</u>	0.03
-14	0.01	< URA <sub>ED</sub>	$\leq$	0.02
-15		$URA_{ED}$	<u>≤</u>	0.01
-16	No accuracy pre	ediction avai	lable-use at o	own risk

For each URA index (N), users may compute a nominal URA value (X) as given by:

- If the value of N is 6 or less,  $X = 2^{(1 + N/2)}$ ,
- If the value of N is 6 or more, but less than 15,  $X = 2^{(N-2)}$ ,
- N = 15 shall indicate the absence of an accuracy prediction and shall advise the standard positioning service user to use that SV at his own risk.

For N = 1, 3, and 5, X should be rounded to 2.8, 5.7, and 11.3 meters, respectively.

The nominal URA<sub>ED</sub> value (X) is suitable for use as a conservative prediction of the RMS ED range errors for accuracy-related purposes in the pseudorange domain (e.g., measurement deweighting, RAIM, FOM computations). Integrity properties of the IAURA<sub>ED</sub> are specified with respect to the scaled (multiplied by either 4.42 or 5.73 as appropriate) upper bound values of the broadcast URA<sub>ED</sub> index (see 20.3.3.1.1).

For the nominal URA<sub>ED</sub> value and the IAURA<sub>ED</sub> value, users may compute an adjusted URA<sub>ED</sub> value as a function of SV elevation angle (E), for  $E \ge 0$ , as follows:

Adjusted Nominal URA<sub>ED</sub> = Nominal URA<sub>ED</sub> (sin(E+90 degrees))

Adjusted IAURA<sub>ED</sub> = IAURA<sub>ED</sub> (sin(E+90 degrees))

URA<sub>ED</sub> and IAURA<sub>ED</sub> account for SIS contributions to user range error which include, but are not limited to, the following: LSB representation/truncation error, alongtrack ephemeris errors, and crosstrack ephemeris errors. URA<sub>ED</sub> and IAURA<sub>ED</sub> do not account for user range error contributions due to the inaccuracy of the broadcast ionospheric data parameters used in the single-frequency ionospheric model or for other atmospheric effects.

**20.3.3.1.2** Message Types 10 and 11 Ephemeris Parameter Characteristics. For each ephemeris parameter contained in message types 10 and 11, the number of bits, the scale factor of the least significant bit (LSB) (which is the last bit received), the range, and the units are as specified in Table 20-I. See Figures 20-1 and 20-2 for complete bit allocation in message types 10 and 11.

**20.3.3.1.3** <u>User Algorithm for Determination of SV Position.</u> The user shall compute the ECEF coordinates of position for the SV's antenna phase center (APC) utilizing a variation of the equations shown in Table 20-II. The ephemeris parameters are Keplerian in appearance; the values of these parameters, however, are produced by the CS (Block IIF) or the SV (GPS III) via a least squares curve fit of the predicted ephemeris of the SV APC (time-position quadruples; t, x, y, z expressed in ECEF coordinates). Particulars concerning the applicable coordinate system are given in Sections 20.3.3.4.3.3 and 20.3.3.4.3.4 of IS-GPS-200.

The sensitivity of the SV's position to small perturbations in most ephemeris parameters is extreme. The sensitivity of position to the parameters A,  $C_{rc-n}$ , and  $C_{rs-n}$  is about one meter/meter. The sensitivity of position to the angular parameters is on the order of  $10^8$  meters/semi-circle, and to the angular rate parameters is on the order of  $10^{12}$  meters/semi-circle/second. Because of this extreme sensitivity to angular perturbations, the value of  $\pi$  used in the curve fit is given here.  $\pi$  is a mathematical constant, the ratio of a circle's circumference to its diameter. Here  $\pi$  is taken as 3.1415926535898.

	Table 20-I. Message Type	s 10 and 11 Pa	rameters (1	of 2)	
Parameter Symbol	Parameter Description	No. of Bits**	Scale Factor (LSB)	Effective Range***	Units
WN	Week No.	13	1		weeks
URA <sub>ED</sub> INDEX	ED accuracy	5*			(see text)
Signal health (L1/L2/L5)		3	1		(see text)
t <sub>op</sub>	Data predict time of week	11	300	604,500	seconds
ΔΑ ****	Semi-major axis difference at reference time	26*	2-9		meters
Å	Change rate in semi-major axis	25*	2 <sup>-21</sup>		meters/sec
$\Delta n_0$	Mean Motion difference from computed value at reference time	17*	2 <sup>-44</sup>		semi- circles/sec
$\Delta \hat{n}_0$	Rate of mean motion difference from computed value	23*	2 <sup>-57</sup>		semi- circles/sec <sup>2</sup>
$ m M_{0-n}$	Mean anomaly at reference time	33*	2 <sup>-32</sup>		semi-circles
$e_n$	Eccentricity	33	2-34	0.03	dimensionless
$\omega_{\mathrm{n}}$	Argument of perigee	33*	2 <sup>-32</sup>		semi-circles

<sup>\*</sup> Parameters so indicated are two's complement, with the sign bit (+ or -) occupying the MSB;

<sup>\*\*</sup> See Figure 20-1 for complete bit allocation in message type 10;

<sup>\*\*\*</sup> Unless otherwise indicated in this column, effective range is the maximum range attainable with indicated bit allocation and scale factor.

<sup>\*\*\*\*</sup> Relative to  $A_{REF} = 26,559,710$  meters.

Table 20-I. Message Types 10 and 11 Parameters (2 of 2)						
Parameter Symbol	Parameter Description	No. of Bits**	Scale Factor (LSB)	Effective Range***	Units	
t <sub>oe</sub>	Ephemeris data reference time of week	11	300	604,500	seconds	
$\Omega_{ extsf{0-n}}$	Longitude of Ascending Node of Orbit Plane at Weekly Epoch	33*	2 <sup>-32</sup>		semi-circles	
ΔΩ ****	Rate of right ascension difference	17*	$2^{-44}$		semi-circles/sec	
i <sub>0-n</sub>	Inclination angle at reference time	33*	2-32		semi-circles	
$i_{0-n}^{\bullet}$	Rate of inclination angle	15*	$2^{-44}$		semi-circles/sec	
$C_{is-n}$	Amplitude of the sine harmonic correction term to the angle of inclination	16*	2-30		radians	
C <sub>ic-n</sub>	Amplitude of the cosine harmonic correction term to the angle of inclination	16*	2-30		radians	
$C_{rs-n}$	Amplitude of the sine correction term to the orbit radius	24*	2-8		meters	
C <sub>re-n</sub>	Amplitude of the cosine correction term to the orbit radius	24*	2-8		meters	
$C_{us-n}$	Amplitude of the sine harmonic correction term to the argument of latitude	21*	2-30		radians	
C <sub>uc-n</sub>	Amplitude of the sine harmonic correction term to the argument of latitude	21*	2-30		radians	

<sup>\*</sup> Parameters so indicated are two's complement, with the sign bit (+ or -) occupying the MSB;

<sup>\*\*</sup> See Figure 20-1 and Figure 20-2 for complete bit allocation in message types 10 and 11;

<sup>\*\*\*</sup> Unless otherwise indicated in this column, effective range is the maximum range attainable with indicated bit allocation and scale factor.

<sup>\*\*\*\*</sup> Relative to  $\Omega_{REF} = -2.6 \text{ x } 10^{-9} \text{ semi-circles/second.}$ 

Table 20-II. Elements of Coordinate System (part 1 of 2)				
Element/Equation	Description			
$\mu = 3.986005 \text{ x } 10^{14} \text{ meters}^3/\text{sec}^2$	WGS 84 value of the earth's gravitational constant for GPS user			
$ \Omega_{\rm e}^{\bullet} = 7.2921151467 \times 10^{-5} \text{ rad/sec} $	WGS 84 value of the earth's rotation rate			
$A_0 = A_{REF} + \Delta A *$	Semi-Major Axis at reference time			
$A_k = A_0 + (\mathring{A}) t_k$	Semi-Major Axis			
$n_0 = \sqrt{\frac{\mu}{A_0^3}}$	Computed Mean Motion (rad/sec)			
$t_k = t - t_{oe} **$	Time from ephemeris reference time			
$\Delta n_A = \Delta n_0 + \frac{1}{2} \Delta n_0^{\bullet} t_k$	Mean motion difference from computed value			
$n_A \ = n_0 + \Delta n_A$	Corrected Mean Motion			
$\mathbf{M}_{\mathbf{k}} = \mathbf{M}_0 + \mathbf{n}_{\mathbf{A}} \; \mathbf{t}_{\mathbf{k}}$	Mean Anomaly			
$M_k = E_k - e_n \sin E_k$	Kepler's equation for Eccentric Anomaly (radians) (may be solved by iteration)			
$v_k = \tan^{-1} \left\{ \frac{\sin v_k}{\cos v_k} \right\}$	True Anomaly			
$= tan^{-1} \left\{ \frac{\sqrt{1 - e_n^2} \sin E_k / (1 - e_n \cos E_k)}{(\cos E_k - e_n) / (1 - e_n \cos E_k)} \right\}$				
$E_k = cos^{-1} \left\{ \frac{e_n + cosv_k}{1 + e_n cosv_k} \right\}$	Eccentric Anomaly			

<sup>\*</sup>  $A_{REF} = 26,559,710 \text{ meters}$ 

<sup>\*\*</sup> **t** is GPS system time at time of transmission, i.e., GPS time corrected for transit time (range/speed of light). Furthermore, t<sub>k</sub> shall be the actual total difference between the time **t** and the epoch time t<sub>oe</sub>, and must account for beginning or end of week crossovers. That is if t<sub>k</sub> is greater than 302,400 seconds, subtract 604,800 seconds from t<sub>k</sub>. If t<sub>k</sub> is less than -302,400 seconds, add 604,800 seconds to t<sub>k</sub>.

Table 20-II. Elements of	Coordinate System (part 2 of 2)		
Element/Equation *	Description		
$\Phi_k = \nu_k + \omega_n$	Argument of Latitude		
$\delta u_k = C_{us-n} sin2\Phi_k + C_{uc-n} cos2\Phi_k$	Argument of Latitude Correction Second Harmonic		
$\delta r_k = C_{rs-n} sin2\Phi_k + C_{rc-n} cos2\Phi_k$	Radial Correction Perturbations		
$\delta i_k = C_{is-n} sin 2\Phi_k + C_{ic-n} cos 2\Phi_k$	Inclination Correction		
$u_k = \Phi_k + \delta u_k$	Corrected Argument of Latitude		
$r_k = A_k(1 - e_n \cos E_k) + \delta r_k$	Corrected Radius		
$i_k = i_{o-n} + (i_{o-n}^{\bullet})t_k + \delta i_k$	Corrected Inclination		
$ x_k' = r_k \cos u_k $ $y_k' = r_k \sin u_k $	Positions in orbital plane		
$ec{\Omega} = ec{\Omega}_{ ext{REF}}^{ullet} + \Delta ec{\Omega}^{ullet} ~***$	Rate of Right Ascension		
$\Omega_{\rm k} = \Omega_{0-\rm n} + (\Omega^{\bullet} - \Omega^{\bullet}_{\rm e}) t_{\rm k} - \Omega^{\bullet}_{\rm e} t_{\rm oe}$	Corrected Longitude of Ascending Node		
$ \left. \begin{array}{l} x_k = x_k' \cos \Omega_k - y_k' \cos i_k \sin \Omega_k \\ \\ y_k = x_k' \sin \Omega_k + y_k' \cos i_k \cos \Omega_k \\ \\ z_k = y_k' \sin i_k \end{array} \right\} $	Earth-fixed coordinates of SV antenna phase center		
*** $\hat{\Omega}_{REF} = -2.6 \times 10^{-9} \text{ semi-circles/second.}$	1		

## 20.3.3.2 Message Types 30 through 37 SV Clock Correction Parameters.

**20.3.3.2.1** Message Types 30 through 37 SV Clock Correction Parameter Content. The clock parameters in any one of message types 30 through 37 describe the SV time scale during the period of validity. The parameters are applicable during the time in which they are transmitted. Beyond that time they are still applicable, however, the most recent data set should be used since the accuracy degrades over time.

The general format of message types 30 through 37 includes data fields for SV clock correction coefficients. Any one of message types 30 through 37 in conjunction with message types 10 and 11 provide users with the requisite data to correct SV time and to calculate SV position precisely.

In general, any message of type 30 to 39 will provide SV clock correction parameters as described in this section.

- **20.3.3.2.1.1 SV Clock Correction.** Any one of message types 30 through 37, Figure 20-3 through Figure 20-10, contains the parameters needed by the users for apparent SV clock correction. Bits 61 to 71 contain  $t_{oc}$ , clock data reference time of week. Bits 72 to 127 contain SV clock correction coefficients. The related algorithm is given in paragraph 20.3.3.2.3.
- **20.3.3.2.1.2** <u>Data Predict Time of Week.</u> Bits 39 through 49 of message types 30 through 37 shall contain the data predict time of week (top). The top term provides the epoch time of week of the state estimate utilized for the prediction of SV clock correction coefficients.
- **20.3.3.2.2** <u>Clock Parameter Characteristics.</u> The number of bits, the scale factors of the LSB (which is the last bit received), the range, and the units of clock correction parameters shall be as specified in Table 20-III.
- **20.3.3.2.3** <u>User Algorithms for SV Clock Correction Data.</u> The algorithms defined in paragraph 20.3.3.3.3.1 of IS-GPS-200 allow all users to correct the code phase time received from the SV with respect to both SV code phase offset and relativistic effects. However, since the SV clock corrections of equations in paragraph 20.3.3.3.3.1 of IS-GPS-200 are estimated by the CS using dual frequency L1 and L2 P(Y) code measurements, the single-frequency L5 user and the dual-frequency L1 and L5, and L2 and L5 users must apply additional terms to the SV clock corrections equations. These terms are described in paragraph 20.3.3.3.1.

	Table 20-III. Clock Correction and Accuracy Parameters					
Parameter Symbol	Parameter Description	No. of Bits**	Scale Factor (LSB)	Effective Range***	Units	
$t_{oc}$	Clock Data Reference Time of Week	11	300	604,500	seconds	
URA <sub>NED</sub> Index	NED Accuracy Index	5*			(see text)	
URA <sub>NED1</sub> Index	NED Accuracy Change Index	3			(see text)	
URA <sub>NED2</sub> Index	NED Accuracy Change Rate Index	3			(see text)	
$a_{f2-n}$	SV Clock Drift Rate Correction Coefficient	10*	2 <sup>-60</sup>		sec/sec <sup>2</sup>	
$a_{\rm fl-n}$		20*	$2^{-48}$		sec/sec	
$a_{ m f0-n}$	SV Clock Drift Correction Coefficient	26*	2-35		seconds	
	SV Clock Bias Correction Coefficient					

<sup>\*</sup> Parameters so indicated are two's complement, with the sign bit (+ or -) occupying the MSB;

20.3.3.2.4 <u>Non-Elevation-Dependent (NED) Accuracy Estimates</u>. Bits 50 through 54, and 55 through 57, and 58 through 60 of message types 30 through 37 shall contain the non-elevation-dependent (NED) component  $URA_{NED0}$  Index,  $URA_{NED1}$  Index, and  $URA_{NED2}$  Index, respectively, of the SV (reference paragraph 6.2.1) for the unauthorized user. The following equations together with the broadcast  $URA_{NED0}$  Index,  $URA_{NED1}$  Index, and  $URA_{NED2}$  Index shall give the clock-related user range accuracy of  $IAURA_{NED}$  over the current clock/ephemeris fit interval. While the actual NED-related URA may vary over the satellite footprint, the  $IAURA_{NED}$  calculated using the parameters in message type 10 at each instant during the current clock/ephemeris fit interval shall bound the maximum  $IAURA_{NED}$  expected for the worst-case location within the satellite footprint at that instant.

The user shall calculate the NED-related URA with the equation (in meters);

$$IAURA_{NED} = URA_{NED0} + URA_{NED1} (t - t_{op} + 604,800*(WN - WN_{op}))$$

for t - 
$$t_{op}$$
 + 604,800\*(WN - WN<sub>op</sub>)  $\leq$  93,600 seconds

$$IAURA_{NED} = URA_{NED0} + URA_{NED1}*(t - t_{op} + 604,800*(WN - WN_{op})) + URA_{NED2}*(t - t_{op} + 604,800*(WN - WN_{op}) - 93,600)^{2}$$

<sup>\*\*</sup> See Figures 20-3 through 20-10 for complete bit allocation in message types 30 to 37;

<sup>\*\*\*</sup> Unless otherwise indicated in this column, effective range is the maximum range attainable with indicated bit allocation and scale factor.

for t -  $t_{op}$  + 604,800\*(WN - WN<sub>op</sub>) > 93,600 seconds

where

t is the GPS system time

 $WN_{op}$  -- Data Predict Week Number, identifying the GPS week to which the  $t_{op}$  term refers. See Section 20.3.3.1.1.3 and 20.3.3.2.1.2 (Data Predict Time of Week).

The CS shall derive  $URA_{NED0}$ ,  $URA_{NED1}$ , and  $URA_{NED2}$  indexes which, when used together in the above equations, results in the minimum  $IAURA_{NED}$  that is greater than the predicted  $IAURA_{NED}$  during the ephemeris fit interval.

The user shall use the broadcast  $URA_{NED0}$  index to derive the  $URA_{NED0}$  value. The  $URA_{NED0}$  index is a signed, two's complement integer in the range of +15 to -16 and has the following relationship to the  $URA_{NED0}$  value:

<u>URA<sub>NED0</sub> Index</u>	<u>Ul</u>	RA <sub>NED0</sub> (meters)		
15	6144.00	< URA <sub>NED0</sub>	(or n	o accuracy prediction is available)
14	3072.00	< URA <sub>NED0</sub>	(OI III ≤	6144.00
13	1536.00	< URA <sub>NED0</sub>	<u> </u>	3072.00
12	768.00	< URA <sub>NED0</sub>		1536.00
11	384.00	< URA <sub>NED0</sub>		768.00
10	192.00	< URA <sub>NED0</sub>		384.00
9	96.00	< URA <sub>NED0</sub>		192.00
8	48.00			96.00
		$<$ URA $_{ m NED0}$	_	
7	24.00	< URA <sub>NED0</sub>		48.00
6	13.65	$<$ URA $_{ m NED0}$	<u> </u>	24.00
5	9.65	$<$ URA $_{ m NED0}$	$\leq$	13.65
4	6.85	$<$ URA $_{ m NED0}$	$\leq$	9.65
3	4.85	$<$ URA $_{ m NED0}$	$\leq$	6.85
2	3.40	$<$ URA $_{ m NED0}$	$\leq$	4.85
1	2.40	$<$ URA $_{ m NED0}$	$\leq$	3.40
0	1.70	$<$ URA $_{ m NED0}$	$\leq$	2.40
1	1.20	$<$ URA $_{ m NED0}$	$\leq$	1.70
-2	0.85	$<$ URA $_{ m NED0}$	<	1.20
-3	0.60	< URA <sub>NED0</sub>	<	0.85
-4	0.43	< URA <sub>NED0</sub>	<	0.60
-5	0.30	< URA <sub>NED0</sub>	<	0.43
-6	0.21	< URA <sub>NED0</sub>		0.30
-7	0.15	< URA <sub>NED0</sub>	_	0.21
-8	0.13	< URA <sub>NED0</sub>	<u>-`</u> ≤	0.15
-0	0.11	< UNANEDO	_	0.13

-9	0.08	$<$ URA $_{ m NED0}$	$\leq$	0.11				
-10	0.06	$<$ URA $_{ m NED0}$	$\leq$	0.08				
-11	0.04	$<$ URA $_{ m NED0}$	$\leq$	0.06				
-12	0.03	$<$ URA $_{ m NED0}$	$\leq$	0.04				
-13	0.02	$<$ URA $_{ m NED0}$	$\leq$	0.03				
-14	0.01	$<$ URA $_{ m NED0}$	$\leq$	0.02				
-15		$URA_{NED0}$	$\leq$	0.01				
-16	No accuracy	No accuracy prediction available-use at own risk						

Integrity properties of the URA are specified with respect to the upper bound values of the URA index (see 20.3.3.1.1).

For each URA<sub>NED0</sub> index (N), users may compute a nominal URA<sub>NED0</sub> value (X) as given by:

- If the value of N is 6 or less, but more than -16,  $X = 2^{(1 + N/2)}$ ,
- If the value of N is 6 or more, but less than 15,  $X = 2^{(N-2)}$ ,
- N = -16 or N = 15 shall indicate the absence of an accuracy prediction and shall advise the standard positioning service user to use that SV at his own risk.

For N = 1, 3, and 5, X should be rounded to 2.8, 5.7, and 11.3 meters, respectively.

The nominal  $URA_{NED0}$  value (X) shall be suitable for use as a conservative prediction of the RMS NED range errors for accuracy-related purposes in the pseudorange domain (e.g., measurement de-weighting RAIM, FOM computations). Integrity properties of the IAURA<sub>NED</sub> are specified with respect to the scaled (multiplied by either 4.42 or 5.73 as appropriate) upper bound values of the  $URA_{NED0}$  index,  $URA_{NED1}$  index, and  $URA_{NED2}$  index (see 20.3.3.1.1).

URA<sub>NED0</sub> accounts for zeroth order SIS-contributions to user range error which include, but are not limited to, the following: LSB representation/truncation error; the net effect of clock correction polynomial error and code phase error in the transmitted signal for single-frequency L1C/A or single-frequency L2C users who correct the code phase as described in Section 20.3.3.3.1.1.1; the net effect of clock parameter, code phase, and inter-signal correction error for dual-frequency L1/L2 and L1/L5 users who correct for group delay and ionospheric effects as described in Section 20.3.3.3.1.1.2; radial ephemeris error; anisotropic antenna errors; and signal deformation error. URA<sub>NED</sub> does not account for user range contributions due to the inaccuracy of the broadcast ionospheric data parameters used in the single-frequency ionospheric model or for other atmospheric effects.

The transmitted  $URA_{NED1}$  index is an integer value in the range 0 to 7. The  $URA_{-NED1}$  index has the following relationship to the  $URA_{-NED1}$  value:

$$URA_{NED1} = \frac{1}{2^{N}}$$
 (meters/second)

where

$$N = 14 + URA_{NED1} Index.$$

The transmitted  $URA_{NED2}$  index is an integer value in the range 0 to 7.  $URA_{NED2}$  index has the following relationship to the  $URA_{NED2}$ :

$$URA_{NED2} = \frac{1}{2^{N}}$$
(meters/second/second)

where

$$N = 28 + URA_{NED2}$$
 Index.

## 20.3.3.3 Message Type 30 Ionospheric and Group Delay Correction Parameters.

## 20.3.3.3.1 Message Type 30 Ionospheric and Group Delay Correction Parameter Content.

Message type 30 provides SV clock correction parameters (ref. Section 20.3.3.2) and ionospheric and group delay correction parameters. Bits 128 through 192 of message type 30 provide the group delay differential correction terms for L1, L2, and L5 signal users. Bits 193 through 256 provide the ionospheric correction parameters for single frequency user. The following algorithms shall apply when interpreting the correction parameters in the message.

**20.3.3.3.1.1** Estimated L1-L2 Group Delay Differential. The group delay differential correction terms,  $T_{GD}$ ,  $ISC_{L1C/A}$ ,  $ISC_{L2C}$  are contained in bits 128 through 166 of message type 30. See paragraph 30.3.3.3.1.1 of IS-GPS-200. The bit lengths, scale factors, ranges, and units of these parameters are given in Table 20-IV. These group delay differential correction terms are also used for the benefit of single frequency L5-I5 and L5-Q5 users and dual frequency L1/L5 and L2/L5 users.

**20.3.3.3.1.1.1** <u>L1/L2 Inter-Signal Group Delay Differential Correction.</u> See paragraph 30.3.3.3.1.1.1 of IS-GPS-200.

**20.3.3.3.1.2** Estimated L5 Group Delay Differential. The group delay differential correction terms,  $T_{GD}$ , ISC<sub>L5I5</sub> and ISC<sub>L5Q5</sub>, for the benefit of single frequency L5-I5 and L5-Q5 users and dual frequency L1/L5 and L2/L5 users are contained in bits 128 through 140 and 167 through 192 of message type 30 (see Figure 20-3 for complete bit allocation). The bit lengths, scale factors, ranges, and units of these parameters are given in Table 20-IV. The bit string of

70

"100000000000" shall indicate that the group delay value is not available. The related algorithms are given in paragraphs 20.3.3.3.1.2.1, 20.3.3.3.1.2.2, and 20.3.3.3.1.2.3.

Table 20-IV. Group Delay Differential Parameters ****					
Parameter	No. of Bits**	Scale Factor (LSB)	Effective Range***	Units	
$T_{ m GD}$	13*	2 <sup>-35</sup>		seconds	
ISC <sub>L1C/A</sub>	13*	2 <sup>-35</sup>		seconds	
$ISC_{L2C}$	13*	2 <sup>-35</sup>		seconds	
ISC <sub>L515</sub>	13*	2 <sup>-35</sup>		seconds	
$ISC_{L5Q5}$	13*	2 <sup>-35</sup>		seconds	

<sup>\*</sup> Parameters so indicated are two's complement with the sign bit (+ or -) occupying the MSB;

**20.3.3.3.1.2.1** <u>L1/L5 Inter-Signal Correction.</u> The L5 correction terms,  $T_{GD}$ , ISC<sub>L5I5</sub> and ISC<sub>L5Q5</sub> are provided by the CS to account for the effect of inter-signal biases between L1 P(Y) and L2 P(Y), L1 P(Y) and L5 I5, and between L1 P(Y) and L5 Q5, respectively. These values are initially based on measurements made by the SV contractor during SV manufacture. The values of  $T_{GD}$  and ISC's for each SV may be subsequently updated to reflect the actual on-orbit group delay differential. For maximum accuracy, the single frequency L5 I5 user must use the correction terms to make further modifications to the code phase offset in paragraph 20.3.3.3.3.1 of IS-GPS-200 with the equation:

$$(\Delta t_{SV})_{L5I5} = \Delta t_{SV} - T_{GD} + ISC_{L5I5}$$

where  $T_{GD}$  (see paragraph 20.3.3.3.3.2 of IS-GPS-200) and ISC<sub>L515</sub> (described in paragraph 20.3.3.3.1.2) are provided to the user as message type 30 data. For maximum accuracy, the single frequency L5 Q5 user must use the correction terms to make further modifications to the code phase offset given by:

$$(\Delta t_{SV})_{L5O5} = \Delta t_{SV} - T_{GD} + ISC_{L5O5}$$

<sup>\*\*</sup> See Figure 20-3 for complete bit allocation in message type 30;

<sup>\*\*\*</sup> Effective range is the maximum range attainable with indicated bit allocation and scale factor;

<sup>\*\*\*\*</sup> The bit string of "100000000000" will indicate that the group delay value is not available.

where  $ISC_{L5Q5}$  (described in paragraph 20.3.3.3.1.2) is provided to the user as message type 30 data.

The values of  $ISC_{L5I5}$  and  $ISC_{L5Q5}$  are measured values that represent the mean SV group delay differential between the L1 P(Y)-code and the L5 I5-code or L5 Q5-code respectively as follows.

$$ISC_{L5I5} = t_{L1P(Y)} - t_{L5I5}$$

$$ISC_{L5Q5} = t_{L1P(Y)} - t_{L5Q5}$$

where  $t_{Lix}$  is the GPS time the  $i^{th}$  frequency x signal (a specific epoch of the signal) is transmitted from the SV antenna phase center.

**20.3.3.3.1.2.2** <u>L1/L5 Ionospheric Correction.</u> The two frequency (L1 C/A and L5 I5) user shall correct for the group delay and ionospheric effects by applying the relationship:

$$PR = \frac{(PR_{L5I5} - \gamma_{15}PR_{LIC/A}) + c(ISC_{L5I5} - \gamma_{15}ISC_{LIC/A})}{1 - \gamma_{15}} - cT_{GD}$$

The two frequency (L1 C/A and L5 Q5) user shall correct for the group delay and ionospheric effects by applying the relationship:

$$PR = \frac{(PR_{L5Q5} - \gamma_{15}PR_{L1C/A}) + c(ISC_{L5Q5} - \gamma_{15}ISC_{L1C/A})}{1 - \gamma_{15}} - cT_{GD}$$

where

PR = pseudorange corrected for ionospheric effects,

PR<sub>i</sub> = pseudorange measured on the channel indicated by the subscript;

 $ISC_i$  = inter-signal correction for the channel indicated by the subscript (see paragraph 20.3.3.3.1.2),

 $T_{GD}$  = see paragraph 20.3.3.3.2 of IS-GPS-200,

c = speed of light (see paragraph 20.3.4.3),

and where, denoting the nominal center frequencies of L1 and L5 as f<sub>L1</sub> and f<sub>L5</sub> respectively,

$$\gamma_{15} = (f_{L1}/f_{L5})^2 = (1575.42/1176.45)^2 = (154/115)^2.$$

**20.3.3.1.2.3 L2/L5 Ionospheric Correction.** The two frequency (L2 C and L5 I5) user shall correct for the group delay and ionospheric effects by applying the relationship:

$$PR = \frac{(PR_{L5I5} - \gamma_{25}PR_{L2C}) + c(ISC_{L5I5} - \gamma_{25}ISC_{L2C})}{1 - \gamma_{25}} - cT_{GD}$$

The two frequency (L2 C and L5 Q5) user shall correct for the group delay and ionospheric effects by applying the relationship:

$$PR = \frac{(PR_{L5Q5} - \gamma_{25}PR_{L2C}) + c(ISC_{L5Q5} - \gamma_{25}ISC_{L2C})}{1 - \gamma_{25}} - cT_{GD}$$

where

PR = pseudorange corrected for ionospheric effects,

PR<sub>i</sub> = pseudorange measured on the channel indicated by the subscript,

 $ISC_i$  = inter-signal correction for the channel indicated by the subscript (see paragraph 20.3.3.3.1.2),

 $T_{GD}$  = see paragraph 20.3.3.3.2 of IS-GPS-200,

c = speed of light (see paragraph 20.3.4.3).

and where, denoting the nominal center frequencies of L2 and L5 as f<sub>L2</sub> and f<sub>L5</sub> respectively.

$$\gamma_{25} = (f_{L2}/f_{L5})^2 = (1227.6/1176.45)^2 = (24/23)^2$$

**20.3.3.3.1.3** <u>Ionospheric Data.</u> The ionospheric parameters which allow the "L5 only" user to utilize the ionospheric model for computation of the ionospheric delay are contained in message type 30. The "one frequency" user should use the model given in Figure 20-4 of IS-GPS-200 to make this correction. The calculated value of  $T_{iono}$  ( $T_{iono}$  = ionospheric correction parameter) in the model is referred to the L1 frequency; if the user is operating on the L5 frequency, the correction term must be multiplied by  $\gamma$ 15 (reference paragraph 20.3.3.3.1.2.2). It is estimated that the use of this model will provide at least a 50 percent reduction in the single-frequency user's RMS error due to ionospheric propagation effects. The bit lengths, scale factors, ranges, and units of these parameters are given in Table 20-X of IS-GPS-200 (See Figure 20-3 for complete ionospheric bit allocation).

The ionospheric data shall be updated by the CS at least once every six days while the CS is able to upload the SVs. If the CS is unable to upload the SVs, the ionospheric data transmitted by the SVs may not be accurate. During extended operations or in the Autonav mode, if the CS is unable to upload the SVs, the use of this model will yield unpredictable results.

**20.3.3.3.1.4** Example Application of Correction Parameters. A typical system application of the correction parameters for a user receiver is shown in Figure 20-15. The ionospheric model referred to in Figure 20-15 is discussed in paragraph 20.3.3.3.1.3.

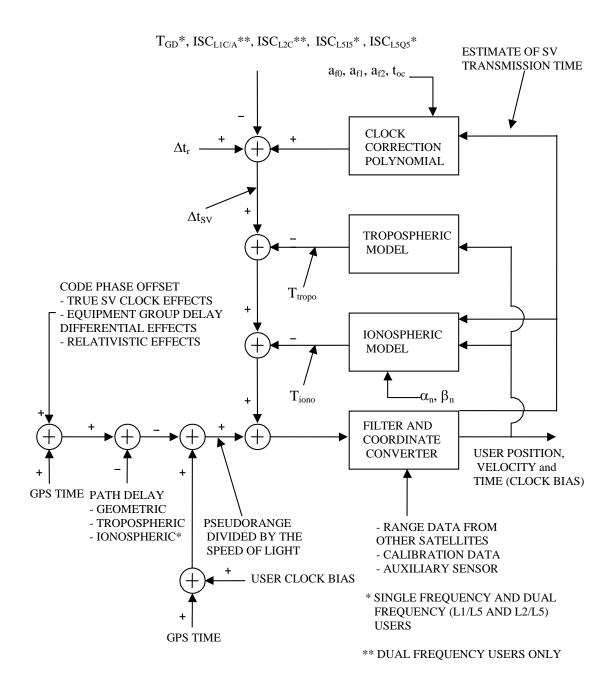


Figure 20-15. Sample Application of Correction Parameters

**20.3.3.4** Message Types 31, 12 and 37 Almanac Parameters. The almanac parameters are provided in any one of message types 31, 37, and 12. Message type 37 provides Midi almanac parameters and the reduced almanac parameters are provided in either message type 31 or type 12. The SV shall broadcast both message types 31 (and/or 12) and 37. However, the reduced almanac parameters (i.e. message types 31 and/or 12) for the complete set of SVs in the constellation will be broadcast by a SV using shorter duration of time compared to the broadcast

of the complete set of Midi almanac parameters (i.e. message type 37). The parameters are defined below, followed by material pertinent to the use of the data.

**20.3.3.4.1** Almanac Reference Week. Bits 39 through 51 of message types 12, and bits 128 through 140 of message type 31 and 37 shall indicate the number of the week (WN<sub>a-n</sub>) to which the almanac reference time ( $t_{oa}$ ) is referenced (see paragraph 20.3.3.4.2). The WN<sub>a-n</sub> term consists of 13 bits which shall be a modulo-8192 binary representation of the GPS week number (see paragraph 6.2.4) to which the  $t_{oa}$  is referenced. Bits 52 through 59 of message types 12, and bits 141 to 148 of message types 31 and 37 shall contain the value of  $t_{oa}$ , which is referenced to this WN<sub>a-n</sub>.

**20.3.3.4.2** Almanac Reference Time. See paragraph 20.3.3.5.2.2 of IS-GPS-200.

**20.3.3.4.3 SV PRN Number.** Bits 149 through 154 of message type 37 and bits 1 through 6 in each packet of reduced almanac shall specify PRN number of the SV whose almanac or reduced almanac, respectively, is provided in the message or in the packet.

**20.3.3.4.4** Signal Health (L1/L2/L5). The three, one-bit, health indication in bits 155, 156 and 157 of message type 37 and bits 29,30 and 31 of each packet of reduced almanac refers to the L1, L2, and L5 signals of the SV whose PRN number is specified in the message or in the packet. For each health indicator, a "0" signifies that all signals on the associated frequency are okay and "1" signifies that some or all signals on the associated frequency are bad. The predicted health data will be updated at the time of upload when a new reduced almanac has been built by the CS. The transmitted health data may not correspond to the actual health of the transmitting SV or other SVs in the constellation.

**20.3.3.4.5** <u>Midi Almanac Parameter Content.</u> Message type 37, Figure 20-10, provides Midi almanac data for a SV whose PRN number is specified in the message. The number of bits, the scale factor (LSB), the range, and the units of the almanac parameters are given in Table 20-V. The user algorithm is essentially the same as the user algorithm used for computing the precise ephemeris as specified in Table 20-IV of IS-GPS-200. Other parameters appearing in the equations of Table 20-IV of IS-GPS-200, but not provided by the Midi almanac with the reference values, are set to zero for SV position determination. See paragraph 20.3.3.5.2.3 of IS-GPS-200 for almanac time parameters.

	Table 20-V. Midi Almanac Parameters							
Parameter	No. of Bits**	Scale Factor (LSB)	Effective Range***	Units				
t <sub>oa</sub>	8	2 <sup>12</sup>	602,112	seconds				
e	11	$2^{-16}$		dimensionless				
$\delta_i^{****}$	11*	$2^{-14}$		semi-circles				
$\dot{\Omega}$	11*	2 <sup>-33</sup>		semi-circles/sec				
$\sqrt{A}$	17	2 <sup>-4</sup>		√meters				
$\Omega_0$	16*	2 <sup>-15</sup>		semi-circles				
ω	16*	2 <sup>-15</sup>		semi-circles				
$\mathbf{M}_0$	16*	2 <sup>-15</sup>		semi-circles				
$a_{ m f0}$	11*	$2^{-20}$		seconds				
$a_{\mathrm{f1}}$	10*	2 <sup>-37</sup>		sec/sec				

<sup>\*</sup> Parameters so indicated shall be two's complement with the sign bit (+ or -) occupying the MSB;

**20.3.3.4.6** Reduced Almanac Parameter Content. Message type 31, Figure 20-4, provides SV clock correction parameters (ref. Section 20.3.3.2) and reduced almanac data packets for 4 SVs. Message type 12, Figure 20-11 contains reduced almanac data packets for 7 SVs.

**20.3.3.4.6.1** Reduced Almanac Data. Message types 31 or 12 contain reduced almanac data and SV health words for SVs in the constellation. The reduced almanac data of a SV is broadcast in a packet 31 bits long, as described in Figure 20-16. The reduced almanac data are a subset of the almanac data which provide less precise ephemeris. The reduced almanac data values are provided relative to pre-specified reference values. The number of bits, the scale factor (LSB), the ranges, and the units of the reduced almanac parameters are given in Table 20-

78

<sup>\*\*</sup> See Figure 20-10 for complete bit allocation in message type 37;

<sup>\*\*\*</sup> Unless otherwise indicated in this column, effective range is the maximum range attainable with indicated bit allocation and scale factor:

<sup>\*\*\*</sup> Relative to  $i_0 = 0.30$  semi-circles.

VI. The algorithms and other material related to the use of the reduced almanac data are given in Section 20.3.3.4.6.2.

The reduced almanac parameters shall be updated by the CS at least once every 3 days while the CS is able to upload the SVs. If the CS is unable to upload the SVs, the accuracy of the reduced almanac parameters transmitted by the SVs will degrade over time.

A 6-bit value of "000000" in the PRN<sub>a</sub> field shall indicate that no further Status Words are contained in the remainder of the data block. In this event, all subsequent bits in the data block field shall be filler bits, i.e., alternating ones and zeros beginning with one.

**20.3.3.4.6.2** Reduced Almanac Packet. The following shall apply when interpreting the data provided in each packet of reduced almanac (see Figure 20-16).

**20.3.3.4.6.2.1** Reduced Almanac. The reduced almanac data is provided in bits 7 through 28 of each packet. The data from a packet along with the reference values (see Table 20-VI) provide ephemeris with further reduced precision. The user algorithm is essentially the same as the user algorithm used for computing the precise ephemeris from the parameters of the message types 10 and 11 (see paragraph 20.3.3.1.3 and Table 20-II). Other parameters appearing in the equations of Table 20-II, but not provided by the reduced almanac with the reference values, are set to zero for SV position determination.

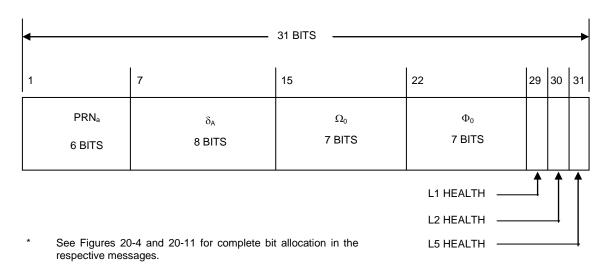


Figure 20-16. Reduced Almanac Packet Content

Table 20-VI. Reduced Almanac Parameters						
Parameter**** No. of Bits Scale Factor (LSB) Effective Range ** Units						
δ <sub>A</sub> ***	8 *	2 <sup>+9</sup>	**	meters		
$\Omega_0$	7 *	2 <sup>-6</sup>	**	semi-circles		
Φ <sub>0</sub> ****	7 *	2 <sup>-6</sup>	**	semi-circles		

- \* Parameters so indicated shall be two's complement with the sign bit (+ or -) occupying the MSB;
- \*\* Effective range is the maximum range attainable with indicated bit allocation and scale factor;
- \*\*\* Relative to  $A_{ref} = 26,559,710$  meters;
- \*\*\*\*  $\Phi_0$  = Argument of Latitude at Reference Time =  $M_0 + \omega$ ;
- \*\*\*\* Relative to following reference values:
  - e = 0
  - $\delta_i = +0.0056$  semi-circles (i = 55 degrees)
  - $\overset{\bullet}{\Omega}$  =-2.6 x 10<sup>-9</sup> semi-circles/second
- **20.3.3.5** <u>Message Type 32 Earth Orientation Parameters (EOP).</u> The earth orientation parameters are provided in message type 32. The parameters are defined below, followed by material pertinent to the use of the data.
- **20.3.3.5.1 EOP Content.** Message type 32, Figure 20-5, provides SV clock correction parameters (ref. Section 20.3.3.2) and earth orientation parameters. The EOP message provides users with parameters to construct the ECEF and ECI coordinate transformation (a simple transformation method is defined in Section 20.3.3.4.3.3.2 of IS-GPS-200). The number of bits, scale factors (LSBs), the ranges, and the units of all EOP fields of message type 32 are given in Table 20-VII.
- **20.3.3.5.1.1** <u>User Algorithm for Application of the EOP</u>. The EOP fields in the message type 32 contain the EOP data needed to construct the ECEF-to-ECI coordinate transformation. The user computes the ECEF position of the SV antenna phase center using the equations shown in Table 20-II. The full coordinate transformation for translating to the corresponding ECI SV antenna phase center position may be accomplished in accordance with the computations detailed in Chapter 5 of IERS Technical Note 36: IERS Conventions (2010) and equations for UT1,  $x_p$  and  $y_p$  as documented in Table 20-VIII. Figure 5.1 on page 73 of that document depicts the computational flow starting from GCRS (Geocentric Celestial Reference System) to ITRS (International Terrestrial Reference System). Ongoing WGS 84 re-adjustment at NGA and incorporating the 2010 IERS Conventions, are expected to bring Earth based coordinate agreement to within 2 cm. In the context of the Conventions, the user may as a matter of

convenience choose to implement the transformation computations via either the "Celestial Intermediate Origin (CIO) based approach" or the "Equinox based approach". The EOP parameters for  $\Delta UT1$  are to be applied within the "Rotation to terrestrial system" process, and the parameters for  $x_p$  and  $y_p$  are applied in the "Rotation for polar motion" process. Users are advised that the broadcast message type 32 EOP parameters already account for zonal, diurnal and semidiurnal effects (described in Chapter 8 of the IERS Conventions (2010)), so these effects should not be further applied by the user.

The relevant computations utilize elementary rotation matrices  $R_i(\alpha)$ , where  $\alpha$  is a positive rotation about the i<sup>th</sup>-axis ordinate, as follows:

$$\mathsf{R}_{1}\left(\alpha\right) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos(\alpha) & \sin(\alpha) \\ 0 & -\sin(\alpha) & \cos(\alpha) \end{bmatrix} \quad , \quad \mathsf{R}_{2}\left(\alpha\right) = \begin{bmatrix} \cos(\alpha) & 0 & -\sin(\alpha) \\ 0 & 1 & 0 \\ \sin(\alpha) & 0 & \cos(\alpha) \end{bmatrix}$$

$$R_{3}(\alpha) = \begin{bmatrix} \cos(\alpha) & \sin(\alpha) & 0 \\ -\sin(\alpha) & \cos(\alpha) & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

The Inertial-to-Geodetic rotation matrix shall be calculated in accordance with the computations detailed in Chapter 5 of IERS Technical Note 36: IERS Conventions (2010) and equations for UT1,  $x_p$  and  $y_p$  as documented in Table 20-VIII.

	Table 20-VII. Ear	th Orienta	tion Paramet	ers	
		No. of	Scale Factor	Effective	
Parameter Symbol	Parameter Description	Bits**	(LSB)	Range***	Units
$t_{ m EOP}$	EOP Data Reference Time	16	$2^4$	604,784	seconds
PM_X <sup>†</sup>	X-Axis Polar Motion Value at Reference Time.	21*	2-20	1	arc-seconds
PM_X	X-Axis Polar Motion Drift at Reference Time.	15*	$2^{-21}$	7.8125 x 10 <sup>-3</sup>	arc-seconds/day
PM_Y <sup>††</sup>	Y-Axis Polar Motion Value at Reference Time.	21*	2-20	1	arc-seconds
PM_Y	Y-Axis Polar Motion Drift at Reference Time.	15*	2 <sup>-21</sup>	7.8125 x 10 <sup>-3</sup>	arc-seconds/day
ΔUT1 <sup>†††</sup>	UT1-UTC Difference at Reference Time.	31*	2 <sup>-24</sup>	64	seconds
ΔUT1 †††	Rate of UT1-UTC Difference at Reference Time	19*	2 <sup>-25</sup>	7.8125 x 10 <sup>-3</sup>	seconds/day

<sup>\*</sup> Parameters so indicated are two's complement, with the sign bit (+ or -) occupying the MSB;

<sup>\*\*</sup> See Figure 20-5 for complete bit allocation in message type 32;

<sup>\*\*\*</sup> Unless otherwise indicated in this column, effective range is the maximum range attainable with indicated bit allocation and scale factor.

<sup>&</sup>lt;sup>†</sup> Represents the predicted angular displacement of instantaneous Celestial Ephemeris Pole with respect to semi-minor axis of the reference ellipsoid along Greenwich meridian.

Represents the predicted angular displacement of instantaneous Celestial Ephemeris Pole with respect to semi-minor axis of the reference ellipsoid on a line directed 90° west of Greenwich meridian.

<sup>†††</sup> With zonal tides restored.

Table 20-VIII. Application of EOP Parameters					
Element/Equation	Description				
$UT1 = UTC + \Delta UT1 + \Delta UT1  (t - t_{EOP})$ $x_P = PM  X + PM  (t - t_{EOP})$	Compute Universal Time at time t  Polar Motion in the x-axis				
$y_p = PM _Y + PMY (t - t_{EOP})$	Polar Motion in the y-axis				

t is GPS system time at time of transmission, i.e., GPS time corrected for transit time (range/speed of light).

**20.3.3.6** <u>Message Type 33 Coordinated Universal Time (UTC) Parameters.</u> Message type 33, Figure 20-6, contains the UTC parameters. The contents of message type 33 are defined below, followed by material pertinent to the use of the UTC data.

**20.3.3.6.1** <u>UTC Parameter Content.</u> Message type 33 provides SV clock correction parameters (ref. Section 20.3.3.2) and also, shall contain the parameters related to correlating UTC (USNO) time with GPS Time. The bit lengths, scale factors, ranges, and units of these parameters are given in Table 20-IX. See Figure 20-6 for complete bit allocation in message type 33.

The parameters relating GPS time to UTC (USNO) shall be updated by the CS at least once every three days while the CS is able to upload the SVs. If the CS is unable to upload the SVs, the accuracy of the UTC parameters transmitted by the SVs will degrade over time.

**20.3.3.6.2** <u>UTC</u> and <u>GPS</u> <u>Time.</u> Message type 33 includes: (1) the parameters needed to relate GPS Time to UTC (USNO), and (2) notice to the user regarding the scheduled future or recent past (relative to NAV message upload) value of the delta time due to leap seconds ( $\Delta t_{LSF}$ ), together with the week number (WN<sub>LSF</sub>) and the day number (DN) at the end of which the leap second becomes effective. Information required to use these parameters to calculate (and define)  $t_{UTC}$  is in paragraph 20.3.3.5.2.4 of IS-GPS-200 except the following definition of  $\Delta t_{UTC}$  shall be used.

 $\Delta t_{UTC} = \Delta t_{LS} + A_{0-n} + A_{1-n} (t_E - t_{ot} + 604,800 (WN - WN_{ot})) + A_{2-n} (t_E - t_{ot} + 604,800 (WN - WN_{ot}))^2$  seconds

	Table 20-	IX. UTC Par	ameters		Table 20-IX. UTC Parameters						
			Scale								
Parameter		No. of	Factor	Effective							
Symbol	Parameter Description	Bits**	(LSB)	Range***	Units						
A <sub>0-n</sub>	Bias coefficient of GPS time scale relative to UTC time scale	16*	2 <sup>-35</sup>		Seconds						
$A_{1-n}$	Drift coefficient of GPS time scale relative to UTC time scale	13*	2 <sup>-51</sup>		sec/sec						
A <sub>2-n</sub>	Drift rate correction coefficient of GPS time scale relative of UTC time scale	7*	2 <sup>-68</sup>		sec/sec <sup>2</sup>						
$\Delta t_{ m LS}$	Current or past leap second count	8*	1		seconds						
t <sub>ot</sub>	Time data reference Time of Week	16	2 <sup>4</sup>	604,784	seconds						
$WN_{ot}$	Time data reference Week Number	13	1		weeks						
$WN_{LSF}$	Leap second reference Week Number	8	1		weeks						
DM		4****	1		days						
DN	Leap second reference Day Number		1		seconds						
$\Delta t_{LSF}$	Current or future leap second count	8*									

<sup>\*</sup> Parameters so indicated shall be two's complement with the sign bit (+ or -) occupying the MSB;

**20.3.3.7** Message Types 34, 13, and 14 Differential Correction Parameters. Differential Correction (DC) parameters are provided either in message type 34, or in types 13 and 14. These parameters provide users with sets of correction terms that apply to the clock and ephemeris data transmitted by other SVs. DC parameters are grouped in packets, as described in the next sections. The availability of these message types is subject to the control and determination of the CS.

**20.3.3.7.1** <u>Differential Correction Parameters Content.</u> Message type 34 provides SV clock correction parameters (ref. Section 20.3.3.2) and also, shall contain DC parameters that apply to the clock and ephemeris data transmitted by another SV. One message type 34, Figure 20-7, shall contain 34 bits of clock differential correction (CDC) parameters and 92 bits of ephemeris differential correction (EDC) parameters for one SV other than the transmitting SV. Bit 150 of message type 34 shall be a DC Data Type indicator that indicates the data type for which the DC

<sup>\*\*</sup> See Figure 20-6 for complete bit allocation

<sup>\*\*\*</sup> Unless otherwise indicated in this column, effective range is the maximum range attainable with indicated bit allocation and scale factor;

<sup>\*\*\*\*</sup> Right justified.

parameters apply. Zero (0) signifies that the corrections apply to L5 CNAV data,  $D_5(t)$ , and one (1) signifies that the corrections apply to NAV data, D(t), described in Appendix II of IS-GPS-200.

Message types 13 and 14 together also provide DC parameters. Message type 13, Figure 20-12, shall contain CDC parameters applicable to 6 SVs and message type 14, Figure 20-13, shall contain EDC parameters applicable to 2 SVs. There shall be a DC Data Type indicator preceding each CDC or EDC packet. The content of an individual data packet is depicted in Figure 20-17. The number of bits, scale factors (LSB), the ranges, and the units of all fields in the DC packet are given in Table 20-X.

**20.3.3.7.2** <u>DC Data Packet.</u> Each DC data packet contains: corrections to SV clock polynomial coefficients provided in any one of the message types 30 to 37 of the corresponding SV; corrections to quasi-Keplerian elements referenced to  $t_{OD}$  of the corresponding SV; User

Differential Range Accuracy (UDRA) and UDRA indices that enable users to estimate the accuracy obtained after corrections are applied. Each DC packet is made up of two different segments. The first segment contains 34 bits for the CDC parameters and the second segment contains 92 bits of EDC parameters totaling 126 bits. The CDC and EDC parameters form an indivisible pair and users must utilize CDC and EDC as a pair. Users must utilize CDC and EDC data pairs of the same  $t_{\text{OD-D}}$  ( $t_{\text{OD-D}}$  =DC data predict time of week) and of the same  $t_{\text{OD}}$ .

- **20.3.3.7.2.1** <u>Differential Correction Data Predict Time of Week.</u> The DC data predict time of week  $(t_{op-D})$  provides the epoch time of week, in increments of 300 seconds (i.e. five minutes), at which the prediction for the associated DC data was performed.
- **20.3.3.7.2.2** <u>Time of Differential Correction Data.</u> The time of DC data, t<sub>OD</sub>, specifies the reference time of week, in increments of 300 seconds (i.e., five minutes) relative to the GPS week, for the associated CDC and EDC data.
- **20.3.3.7.2.3 SV PRN Identification.** The PRN ID of both CDC and EDC of Figure 20-17 identifies the satellite to which the subject 126-bit differential correction packet data applies (by PRN code assignment). A value of all ones "11111111" in any PRN ID field shall indicate that no DC data is contained in the remainder of the data block. In this event, the remainder of the data block shall be filler bits, i.e., alternating ones and zeros beginning with one.

MSB	CDC = Clock Differential Correction		
1	9	22	30 34
PRN ID	δa <sub>f0</sub>	$\delta a_{f1}$	UDRA
8 BITS	13 BITS	8 BITS	5 BITS

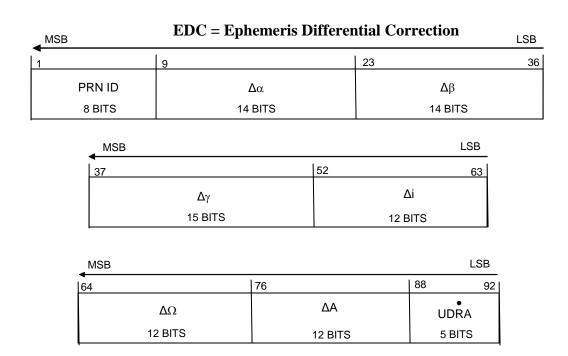


Figure 20-17. Differential Correction Data Packet

	Table 20-X. Differential Correction Parameters						
Parameter Symbol	Parameter Description	No. of Bits**	Scale Factor (LSB)	Effective Range***	Units		
PRN ID	•	8	,		see text		
$\delta a_{ m f0}$	SV Clock Bias Correction	13*	2 <sup>-35</sup>		seconds		
$\delta a_{f1}$	SV Clock Drift Correction	8*	2 <sup>-51</sup>		seconds/second		
UDRA	User Differential Range Accuracy Index.	5*			see text		
Δα	Alpha Correction to Ephemeris Parameters	14*	2 <sup>-34</sup>		dimensionless		
Δβ	Beta Correction to Ephemeris Parameters	14*	2 <sup>-34</sup>		dimensionless		
Δγ	Gamma Correction to Ephemeris Parameters	15*	2 <sup>-32</sup>		semi-circles		
Δί	Angle of Inclination Correction	12*	2-32		semi-circles		
ΔΩ	Angle of Right Ascension Correction	12*	2-32		semi-circles		
ΔΑ	Semi-Major Correction	12*	2 <sup>-9</sup>		meters		
UDRA	Change Rate of User Differential Range Accuracy Index	5*			see text		

<sup>\*</sup> Parameters so indicated are two's complement, with the sign bit (+ or -) occupying the MSB;

**20.3.3.7.3** <u>Application of Clock-Related Differential Correction Data.</u> The SV PRN code phase offset, uncorrected by clock correction coefficient updates, is given by equation 2 in 20.3.3.3.3.1 of IS-GPS-200 (see paragraph 20.3.3.2.3). If the matched pair of DC data for the subject SV is available, the user may apply clock correction coefficient update values by;

$$\Delta t_{sv} = (a_{f0} + \delta a_{f0}) + (a_{f1} + \delta a_{f1})(t - t_{oc}) + a_{f2}(t - t_{oc})^2 + \Delta t_r$$

<sup>\*\*</sup> See Figures 20-7, 11 and 12 for complete bit allocation in message types 34, 13 and 14.

<sup>\*\*\*</sup> Unless otherwise indicated in this column, effective range is the maximum range attainable with indicated bit allocation and scale factor.

where  $\delta a_{f0}$  and  $\delta a_{f1}$ , (see Table 20-X), are given in message types 34 or 13, and all other terms are as stated in 20.3.3.3.3.1 of IS-GPS-200. Clock-related DC data shall not be applied to any SV transmitting clock correction parameters message(s) containing a  $t_{op}$  value greater than the  $t_{op-D}$  value of messages types 34 or 13 containing the clock-related DC data.

**20.3.3.7.4** Application of Orbit-Related Differential Correction Data. The DC data packet includes corrections to parameters that correct the state estimates for ephemeris parameters transmitted in the message types 10 and 11 (broadcast by the SV to which the DC data packet applies). The user will update the ephemeris parameters utilizing a variation of the algorithm expressed in the following equations. The user will then incorporate the updated quasi-Keplerian element set in all further calculations of SV position, as represented by the equations in Table 20-II (see para. 20.3.3.1.3). Ephemeris-related DC data shall not be applied to any SV transmitting message types 10 and 11 containing a t<sub>op</sub> value greater than the t<sub>op-D</sub> value of message types 34 or 14 containing the ephemeris-related DC data.

The user will construct a set of initial (uncorrected) elements by:

$$A_i = A_0$$

$$e_i = e_n$$

$$i_i = i_{0-n}$$

$$\Omega_{\rm i} = \Omega_{0-n}$$

$$\alpha_i = e_n \cdot \cos(\omega_n)$$

$$\beta_i = e_n \cdot \sin(\omega_n)$$

$$\gamma_i = M_{0-n} + \omega_n$$

where  $A_0$ ,  $e_n$ ,  $i_{0-n}$ ,  $\Omega_{0-n}$ ,  $\omega_n$  and  $M_{0-n}$  are obtained from the applicable SV's message types 10 and 11 data. The terms  $\alpha_i$ ,  $\beta_i$ , and  $\gamma_i$  form a subset of stabilized ephemeris elements which are subsequently corrected by  $\Delta\alpha$ ,  $\Delta\beta$  and  $\Delta\gamma$ —the values of which are supplied in the message types 34 or 14-as follows:

88

$$\alpha_c = \alpha_i + \Delta \alpha$$

$$\beta_c = \beta_i + \Delta \beta$$

$$\gamma_c = \gamma_i + \Delta \gamma$$

The quasi-Keplerian elements are then corrected by

$$A_{c} = A_{i} + \Delta A$$

$$e_{c} = (\alpha_{c}^{2} + \beta_{c}^{2})^{1/2}$$

$$i_{c} = i_{i} + \Delta i$$

$$\Omega_{c} = \Omega_{i} + \Delta \Omega$$

$$\omega_{c} = \tan^{-1}(\beta_{c}/\alpha_{c})$$

$$M_{0,c} = \gamma_{c} - \omega_{c} + \Delta M_{0}$$

where  $\Delta A$ ,  $\Delta i$  and  $\Delta \Omega$  are provided in the EDC data packet of the message type 34 or 14 and  $\Delta M_0$  is obtained from

$$\Delta M_0 = \frac{-3}{2} \left( \frac{\mu}{A_0^3} \right)^{\frac{1}{2}} \left( \frac{\Delta A_0}{A_0} \right) \left[ \left( t_{oe} + WN_{oe} * 604,800 \right) - \left( t_{OD} + WN * 604,800 \right) \right]$$

The corrected quasi-Keplerian elements above are applied to the user algorithm for determination of antenna phase center position in Section 20.3.3.1.3, Table 20-II.

**20.3.3.7.5 SV Differential Range Accuracy Estimates.** The UDRA<sub>op-D</sub> and UDRA shall give the differential user range accuracy for the SV. It must be noted that the two parameters provide estimated accuracy after both clock and ephemeris DC are applied. The UDRA<sub>op-D</sub> and UDRA indices are signed, two's complement integers in the range of  $\pm 15$  to  $\pm 16$  and have the

UDRA indices are signed, two's complement integers in the range of +15 to -16 and have the following relationship:

Index Value	<u>UDRA<sub>op-D</sub> (meters)</u>		$UDRA (10^{-6} \text{ m/sec})$
15	$6144.00 < UDRA_{op-D}$	6144.00	
14	$3072.00  <  \mathrm{UDRA}_{\mathrm{op\text{-}D}}$	$\leq$ 6144.00	3072.00
13	$1536.00 < UDRA_{op-D}$	$\leq 3072.00$	1536.00
12	$768.00 < UDRA_{op-D}$	$\leq 1536.00$	768.00
11	$384.00 < UDRA_{op-D}$	≤ 768.00	384.00
10	$192.00 < UDRA_{op-D}$	$\leq 384.00$	192.00
9	$96.00 < UDRA_{op-D}$	≤ 192.00	96.00
8	$48.00 < UDRA_{op-D}$	≤ 96.00	48.00

89

7	24.00	$< UDRA_{op-D}$	$\leq 48.00$	24.00
6	13.65	$< UDRA_{op-D}$	$\leq 24.00$	13.65
5	9.65	$< UDRA_{op-D}$	≤ 13.65	9.65
4	6.85	$< UDRA_{op-D}$	≤ 9.65	6.85
3	4.85	$< UDRA_{op-D}$	$\leq 6.85$	4.85
2	3.40	$< UDRA_{op-D}$	≤ 4.85	3.40
1	2.40	$< UDRA_{op-D}$	≤ 3.40	2.40
0	1.70	$< UDRA_{op-D}$	$\leq 2.40$	1.70
-1	1.20	$< UDRA_{op-D}$	≤ 1.70	1.20
-2	0.85	$< UDRA_{op-D}$	≤ 1.20	0.85
-3	0.60	$< UDRA_{op-D}$	$\leq 0.85$	0.60
-4	0.43	$< UDRA_{op-D}$	$\leq 0.60$	0.43
-5	0.30	$< UDRA_{op-D}$	≤ 0.43	0.30
-6	0.21	$< UDRA_{op-D}$	≤ 0.30	0.21
-7	0.15	$< UDRA_{op-D}$	≤ 0.21	0.15
-8	0.11	$< UDRA_{op-D}$	≤ 0.15	0.11
-9	0.08	$< UDRA_{op-D}$	≤ 0.11	0.08
-10	0.06	$< UDRA_{op-D}$	$\leq 0.08$	0.06
-11	0.04	$< UDRA_{op-D}$	≤ 0.06	0.04
-12	0.03	$< UDRA_{op-D}$	$\leq 0.04$	0.03
-13	0.02	$< UDRA_{op-D}$	≤ 0.03	0.02
-14	0.01	$< UDRA_{op-D}$	$\leq 0.02$	0.01
-15		$\mathrm{UDRA}_{\mathrm{op-D}}$	$\leq 0.01$	0.005
-16	No acc	uracy prediction avail	lable-use at own risk	

For any time, t<sub>k</sub>, other than t<sub>op-D</sub>, UDRA is found by,

$$UDRA = UDRA_{op-D} + UDRA_{(t_k - t_{op-D})}$$

**20.3.3.8** <u>Message Type 35 GPS/GNSS Time Offset.</u> Message type 35, Figure 20-8, contains the GPS/Global Navigation Satellite System (GNSS) Time Offset (GGTO) parameters. The contents of message type 35 are defined below. The validity period of the GGTO shall be 1 day as a minimum.

**20.3.3.8.1** GPS/GNSS Time Offset Parameter Content. Message Type 35 provides SV clock correction parameters (ref. Section 20.3.3.2) and also, shall contain the parameters related to correlating GPS time with other GNSS time. Bits 155 through 157 of message type 35 shall

identify the other GPS-like navigation system to which the offset data applies. The three bits are defined as follows;

000 = no data available,

001 = Galileo,

010 = GLONASS,

011 through 111 = reserved for other systems.

The number of bits, the scales factor (LSB), the ranges, and the units of the GGTO parameters are given in Table 20-XI. See Figure 20-8 for complete bit allocation in message type 35.

20.3.3.8.2 GPS and GNSS Time. The GPS/GNSS-time relationship is given by,

 $t_{GNSS} = t_E - (A_{0GGTO} + A_{1GGTO} (t_E - t_{GGTO} + 604800 (WN - WN_{GGTO})) + A_{2GGTO} (t_E - t_{GGTO} + 604800 (WN - WN_{GGTO}))^2)$ 

where  $t_{GNSS}$  is in seconds,  $t_E$  and WN are as defined in Section 20.3.3.5.2.4 of IS-GPS-200, and the remaining parameters are as defined in Table 20-XI.

Table 20-XI. GPS/GNSS Time Offset Parameters					
Parameter		No. of	Scale Factor	Effective	
Symbol	Parameter Description	Bits**	(LSB)	Range***	Units
$A_{0GGTO}$	Bias coefficient of GPS time scale relative to GNSS time scale	16*	2 <sup>-35</sup>		seconds
$ m A_{1GGTO}$	Drift coefficient of GPS time scale relative to GNSS time scale	13*	2 <sup>-51</sup>		sec/sec
$ m A_{2GGTO}$	Drift rate correction coefficient of GPS time scale relative to GNSS time scale	7*	2 <sup>-68</sup>		sec/sec <sup>2</sup>
$t_{ m GGTO}$	Time data reference Time of Week	16	$2^4$	604,784	seconds
$WN_{GGTO}$	Time data reference Week	13	$2^0$		weeks
GNSS ID	Number GNSS Type ID	3			see text

<sup>\*</sup> Parameters so indicated shall be two's complement with the sign bit (+ or -) occupying the MSB;

<sup>\*\*</sup> See Figure 20-8 for complete bit allocation;

<sup>\*\*\*</sup> Unless otherwise indicated in this column, effective range is the maximum range attainable with indicated bit allocation and scale factor.

**20.3.3.9** Message Types 36 and 15 Text Messages. Text messages are provided either in message type 36, Figure 20-9, or type 15, Figure 20-14. The specific contents of text message will be at the discretion of the Operating Command. Message type 36 can accommodate the transmission of 18 eight-bit ASCII characters. Message type 15 can accommodate the transmission of 29 eight-bit ASCII characters. The requisite bits shall occupy bits 39 through 274 of message type 15 and bits 128 through 275 of message type 36. The eight-bit ASCII characters shall be limited to the set described in paragraph 20.3.3.5.1.8 of IS-GPS-200.

## **20.3.4** <u>Timing Relationships.</u> The following conventions shall apply.

**20.3.4.1** <u>Paging and Cutovers.</u> Broadcast system of messages is completely arbitrary, but sequenced to provide optimum user performance. Message types 10 and 11 shall be broadcast at least once every 24 seconds. All other messages shall be broadcast in-between, not exceeding the maximum broadcast interval in Table 20-XII. Message type 15 will be broadcast as needed, but will not reduce the maximum broadcast interval of the other messages. Type 15 messages that are longer than one page will not necessarily be broadcast consecutively.

Table 20-XII. Message Broadcast Intervals			
Message Data	Message Type Number	Maximum Broadcast Intervals †	
Ephemeris	10 & 11	24 sec	
Clock	Type 30-37	24 sec	
ISC, IONO	30 *	144 sec	
Reduced Almanac	31* or 12	10 min**	
Midi Almanac	37	60 min**	
EOP	32*	15 min	
UTC	33*	144 sec	
Diff Correction	34* or 13 & 14	15 min***	
GGTO	35*	144 sec	
Text	36* or 15	As needed	

<sup>\*</sup> Also contains SV clock correction parameters.

<sup>\*\*</sup> Complete set of SVs in the constellation.

<sup>\*\*\*</sup> When Differential Corrections are available.

<sup>&</sup>lt;sup>†</sup> The intervals specified are maximum. As such, the broadcast intervals may be shorter than the specified value.

**20.3.4.2 SV Time vs. GPS Time.** In controlling the SVs and uploading of data, the CS shall allow for the following timing relationships:

- a. Each SV operates on its own SV time;
- b. All time-related data (TOW) in the messages shall be in SV-time;
- c. All other data in the NAV message shall be relative to GPS time;
- d. The acts of transmitting the NAV messages shall be executed by the SV on SV time.

**20.3.4.3 Speed of Light.** The speed of light used by the CS for generating the data described in the above paragraphs is

 $c = 2.99792458 \times 10^8$  meters per second

which is the official WGS 84 speed of light. The user shall use the same value for the speed of light in all computations.

**20.3.4.4** <u>Data Sets.</u> The  $t_{oe}$  shall be equal to the  $t_{oc}$  of the same CNAV data set. The following rules govern the transmission of  $t_{oe}$  and  $t_{oc}$  values in different data sets: (1) The transmitted  $t_{oc}$  will be different from any value transmitted by the SV during the preceding seven days; (2) The transmitted  $t_{oe}$  will be different from any value transmitted by the SV during the preceding six hours.

Cutovers to new data sets will occur only on hour boundaries except for the first data set of a new upload. The first data set may be cut-in (reference paragraph 20.3.4.1) at any time during the hour and therefore may be transmitted by the SV for less than one hour.

The start of the transmission interval for each data set corresponds to the beginning of the curve fit interval for the data set. Each data set remains valid for the duration of its transmission interval, and nominally also remains valid for the duration of its curve fit interval. A data set is rendered invalid before the end of its curve fit interval when it is superseded by the SV cutting over to the first data set of a new upload.

Normal Operations. The message type 10, 11, and 30-37 data sets are transmitted by the SV for periods of two hours. The corresponding curve fit interval is three hours.

**20.3.4.5** <u>Reference Times</u>. The LNAV reference time information in paragraph 20.3.4.5 in IS-GPS-200 also applies to the CNAV reference times.

**20.3.5 <u>Data Frame Parity.</u>** The data signal contains parity coding according to the following conventions.

**20.3.5.1** Parity Algorithm. Twenty-four bits of CRC parity will provide protection against burst as well as random errors with a probability of undetected error  $\leq 2^{-24} = 5.96 \times 10^{-8}$  for all channel bit error probabilities  $\leq 0.5$ . The CRC word is calculated in the forward direction on a given message using a seed of 0. The sequence of 24 bits (p1,p2,...,p24) is generated from the sequence of information bits (m1,m2,...,m276) in a given message. This is done by means of a code that is generated by the polynomial.

$$g(X) = \sum_{i=0}^{24} g_i X^i$$

where

$$g_i = 1$$
 for  $i = 0, 1, 3, 4, 5, 6, 7, 10, 11, 14, 17, 18, 23, 24= 0 otherwise$ 

This code is called CRC-24Q. The generator polynomial of this code is in the following form (using binary polynomial algebra):

$$g(X) = (1+X)p(X)$$

where p(X) is the primitive and irreducible polynomial

$$p(X) = X^{23} + X^{17} + X^{13} + X^{12} + X^{11} + X^{9} + X^{8} + X^{7} + X^{5} + X^{3} + 1$$

When, by the application of binary polynomial algebra, the above g(X) is divided into  $m(X)X^{24}$ , where the information sequence m(X) is expressed as

$$m(X) = m_k + m_{k-1}X + m_{k-2}X^2 + \cdots + m_1X^{k-1}$$

The result is a quotient and a remainder R(X) of degree < 24. The bit sequence formed by this remainder represents the parity check sequence. Parity bit  $p_i$ , for any i from 1 to 24, is the coefficient of  $x^{24-i}$  in R(X).

This code has the following characteristics:

- 1) It detects all single bit errors per code word.
- 2) It detects all double bit error combinations in a codeword because the generator polynomial g(X) has a factor of at least three terms.
- 3) It detects any odd number of errors because g(X) contains a factor 1+X.
- 4) It detects any burst error for which the length of the burst is  $\leq 24$  bits.
- 5) It detects most large error bursts with length greater than the parity length r = 24 bits. The fraction of error bursts of length b > 24 that are undetected is:

a) 
$$2^{-24} = 5.96 \times 10^{-8}$$
, if  $b > 25$  bits.

b) 
$$2^{-23} = 1.19 \times 10^{-7}$$
, if  $b = 25$  bits.