## CHANGE NOTICE

| Affected Document: | IRN/SCN Number <br> IS-GPS-800 Rev F | IRN-IS-800F-002 |
| :--- | :--- | :--- |
| Authority: | Proposed Change Notice |  |
| RFC-00395 | PCN-IS-800F_RFC395 |  |

## IS800-15 :

## Section Number :

### 2.1.0-4

WAS :
Other Publications

| IS-GPS-200 (current issue) | Navstar GPS Space Segment/Navigation User |
| :--- | :--- |
|  | Interfaces |
| GP-03-001A (20 April 2006) | GPS Interface Control Working Group Charter |

## Redlines:

Other Publications

| IS-GPS-200 (current issue) | Navstar GPS Space Segment/Navigation User |
| :---: | :--- |
|  | Interfaces |
| GP-03-001A (20 April | GPS Interface Control Working Group Chater GPS |
| 2006Current Issue) | $\underline{\text { Adjudication Working Group (AWG) and Rough Order }}$ |
|  | $\underline{\text { of Magnitude (ROM)/ Impact Assessment (IA) Charter }}$ |

## IS:

Other Publications

IS-GPS-200 (current issue)

GP-03-001A (Current Issue)
Navstar GPS Space Segment/Navigation User Interfaces

GPS Adjudication Working Group (AWG) and Rough Order of Magnitude (ROM)/ Impact Assessment (IA) Charter

## IS800-1020 :

Insertion after object IS800-179
The user shall compute the ECEF coordinates of position for the SV's antenna phase center (APC) utilizing a variation of the equations shown in Table 3.5-2. The ephemeris parameters are Keplerian in appearance; however, the values of these parameters are produced by the SV via a least squares curve fit of the propagated ephemeris of the SV APC (timeposition quadruples: $t, x, y, z$ expressed in ECEF coordinates). Particulars concerning the applicable coordinate system are given in Sections 20.3.3.4.3.3 and 20.3.3.4.3.4 of IS-GPS-200.

## Section Number :

### 3.5.3.6.1.1

## WAS :

N/A

## Redlines:

<INSERTED OBJECT>
IS :
The user can compute velocity and acceleration for the SV utilizing a variation of the equations, as required, shown in Table 3.5-2 Part 3 and 4.

## IS800-948 :

## Section Number :

### 3.5.3.6.1.1-2

## WAS :

Table 3.5-2. Elements of Coordinate System (part 1 of 2)

## Redlines

Table 3.5-2._Elements of Broadcast Goordinate Navigation SystemUser Equations (partsheet 1 of Z $\underline{4}$ )
IS :
Table 3.5-2. Broadcast Navigation User Equations (sheet 1 of 4)

## Section Number :

3.5.3.6.1.1-3

WAS :
Table 3.5-2

| Element/Equation | Description |
| :---: | :---: |
| $\mu=3.986005 \times 10^{14}$ meters $^{3} / \mathrm{sec}^{2}$ | WGS 84 value of the earth's gravitational constant for GPS user |
| $\dot{\Omega}_{\mathrm{e}}=7.2921151467 \times 10^{-5} \mathrm{rad} / \mathrm{sec}$ | WGS 84 value of the earth's rotation rate |
| $\mathrm{A}_{0}=\mathrm{A}_{\text {REF }}+\Delta \mathrm{A}^{*}$ | Semi-Major Axis at reference time |
| $\mathrm{A}_{\mathrm{k}}=\mathrm{A}_{0}+(\dot{\mathrm{A}}) \mathrm{t}_{\mathrm{k}}$ | Semi-Major Axis |
| $\mathrm{n}_{0}=\sqrt{\frac{\mu}{\mathrm{A}_{0}{ }^{3}}}$ | Computed Mean Motion (rad/sec) |
| $\mathrm{t}_{\mathrm{k}}=\mathrm{t}-\mathrm{t}_{\text {oe }} * *$ | Time from ephemeris reference time |
| $\Delta \mathrm{n}_{\mathrm{A}}=\Delta \mathrm{n}_{0}+1 / 2 \Delta \mathrm{n}_{0} \mathrm{t}_{\mathrm{k}}$ | Mean motion difference from computed value |
| $\mathrm{n}_{\mathrm{A}}=\mathrm{n}_{0}+\Delta \mathrm{n}_{\mathrm{A}}$ | Corrected Mean Motion |
| $\mathrm{M}_{\mathrm{k}}=\mathrm{M}_{0}+\mathrm{n}_{\mathrm{A}} \mathrm{t}_{\mathrm{k}}$ | Mean Anomaly |
| $\mathrm{M}_{\mathrm{k}}=\mathrm{E}_{\mathrm{k}}-\mathrm{e}_{\mathrm{n}} \sin \mathrm{E}_{\mathrm{k}}$ | Kepler's equation for Eccentric Anomaly (radians) (may be solved by iteration) |
| $v_{\mathrm{k}}=\tan ^{-1}\left\{\frac{\sin v_{\mathrm{k}}}{\cos v_{\mathrm{k}}}\right\}$ | True Anomaly |
| $=\tan ^{-1}\left\{\frac{\sqrt{1-\mathrm{e}_{\mathrm{n}}^{2}} \sin \mathrm{E}_{\mathrm{k}} /\left(1-\mathrm{e}_{\mathrm{n}} \cos \mathrm{E}_{\mathrm{k}}\right)}{\left(\cos \mathrm{E}_{\mathrm{k}}-\mathrm{e}_{\mathrm{n}}\right) /\left(1-\mathrm{e}_{\mathrm{n}} \cos \mathrm{E}_{\mathrm{k}}\right)}\right\}$ |  |
| $E_{k}=\cos ^{-1}\left\{\frac{e_{n}+\cos v_{k}}{1+e_{n} \cos v_{k}}\right\}$ | Eccentric Anomaly |

* $\quad \mathrm{A}_{\text {REF }}=26,559,710$ meters
** $\mathbf{t}$ is GPS system time at time of transmission, i.e., GPS time corrected for transit time (range/speed of light). Furthermore, $\mathrm{t}_{\mathrm{k}}$ shall be the actual total difference between the time $\mathbf{t}$ and the epoch time $\mathrm{t}_{\mathrm{oe}}$, and must account for beginning or end of week crossovers. That is if $t_{k}$ is greater than 302,400 seconds, subtract 604,800 seconds from $t_{k}$. If $t_{k}$ is less than -302,400 seconds, add 604,800 seconds to $t_{k}$.


## Redlines:

Table 3.5-2

| Element/Equation | Description |
| :---: | :---: |
| $\mu=3.986005 \times 10^{14} \mathrm{~meters}^{3} / \mathrm{sec}^{2}$ | WGS 84 value of the earth's gravitational constant for GPS user |
| $\dot{\Omega}_{\mathrm{e}}=7.2921151467 \times 10^{-5} \mathrm{rad} / \mathrm{sec}$ | WGS 84 value of the earth's rotation rate |
| $\mathrm{A}_{0}=\mathrm{A}_{\text {REF }}+\Delta \mathrm{A} *$ | Semi-Major Axis at reference time |
| $\mathrm{A}_{\mathrm{k}}=\mathrm{A}_{0}+(\dot{\mathrm{A}}) \mathrm{t}_{\mathrm{k}}$ | Semi-Major Axis |
| $\mathrm{n}_{0}=\sqrt{\frac{\mu}{\mathrm{A}^{3}}}$ | Computed Mean Motion (rad/sec) |
| $\mathrm{t}_{\mathrm{k}}=\mathrm{t}-\mathrm{t}_{\mathrm{oe}}$ ** | Time from ephemeris reference time |
| $\Delta \mathrm{n}_{\mathrm{A}}=\Delta \mathrm{n}_{0}+1 / 2 \Delta \mathbf{n}_{0} \mathrm{t}_{\mathrm{k}}$ | Mean motion difference from computed value |
| $\mathrm{n}_{\mathrm{A}}=\mathrm{n}_{0}+\Delta \mathrm{n}_{\mathrm{A}}$ | Corrected Mean Motion |
| $\mathrm{M}_{\mathrm{k}}=\mathrm{M}_{0}+\mathrm{n}_{\mathrm{A}} \mathrm{t}_{\mathrm{k}}$ | Mean Anomaly |
| $\mathrm{M}_{k}=\mathrm{E}_{k}-\mathrm{e}_{\mathrm{H}} \sin \mathrm{E}_{k}$ | Kepler's equation for Eccentric Anomaly (radians) (may be solved by iteration) |
|  | Kepler's equation $\left(M_{k}=E_{k}-e \sin E_{k}\right)$ solved for Eccentric anomaly $\left(E_{k}\right)$ by iteration: |
| $\underline{\underline{E}} \underline{0}=\mathrm{M}_{\underline{\underline{k}}}$ | - Initial Value (radians) |
| $E_{j}=E_{j-1}+\frac{M_{k}-E_{j-1}+e \sin E_{j-1}}{1-e \cos E_{j-1}}$ | - Refined Value, three iterations, ( $\mathrm{j}=1,2,3$ ) |
| $\underline{E}_{\underline{k}}=\mathrm{E}_{\underline{3}}$ | - Final Value (radians) |
| $\begin{aligned} & \forall_{k}=\tan ^{-}\left\{\frac{\sin v_{k}}{\left\{\cos v_{k}\right.}\right\} \\ & \left.=\tan ^{-} \frac{\left(\sqrt{1-e_{\#}^{2}} \sin E_{k} /\left(1-e_{n} \cos E_{k}\right)\right.}{\left(\cos E_{k}-e_{H}\right) /\left(1-e_{A} \cos E_{k}\right)}\right\} \end{aligned}$ | True Anomaly |
| $\underline{v}_{\underline{k}}=2 \tan ^{-1}\left(\sqrt{\frac{1+e}{1-e}} \tan \frac{E_{k}}{2}\right)$ | True Anomaly (unambiguous quadrant) |
| $\mathrm{E}_{k}=\cos ^{-1}\left\{\frac{e_{n}+\cos v_{k}}{1+e_{\pi} \cos v_{k}}\right\}$ | Eceentric Amomaly |

* $\quad \mathrm{A}_{\text {ReF }}=26,559,710$ meters
** $\mathbf{t}$ is GPS system time at time of transmission, i.e., GPS time corrected for transit time (range/speed of light). Furthermore, $\mathrm{t}_{\mathrm{k}}$ shall be the actual total difference between the time $\mathbf{t}$ and the epoch time $\mathrm{t}_{\mathrm{oe}}$, and must account for beginning or end of week crossovers. That is if $t_{k}$ is greater than 302,400 seconds, subtract 604,800 seconds from $t_{k}$. If $t_{k}$ is less than -302,400 seconds, add 604,800 seconds to $t_{k}$.

IS :
Table 3.5-2

| Element/Equation | Description |
| :---: | :---: |
| $\mu=3.986005 \times 10^{14} \mathrm{~meters}^{3} / \mathrm{sec}^{2}$ | WGS 84 value of the earth's gravitational constant for GPS user |
| $\dot{\Omega}_{\mathrm{e}}=7.2921151467 \times 10^{-5} \mathrm{rad} / \mathrm{sec}$ | WGS 84 value of the earth's rotation rate |
| $\mathrm{A}_{0}=\mathrm{A}_{\text {REF }}+\Delta \mathrm{A}^{*}$ | Semi-Major Axis at reference time |
| $\mathrm{A}_{\mathrm{k}}=\mathrm{A}_{0}+(\dot{\mathrm{A}}) \mathrm{t}_{\mathrm{k}}$ | Semi-Major Axis |
| $\mathrm{n}_{0}=\sqrt{\frac{\mu}{\mathrm{A}_{0}{ }^{3}}}$ | Computed Mean Motion (rad/sec) |
| $\mathrm{t}_{\mathrm{k}}=\mathrm{t}-\mathrm{t}_{\text {oe }} * *$ | Time from ephemeris reference time |
| $\Delta \mathrm{n}_{\mathrm{A}}=\Delta \mathrm{n}_{0}+1 / 2 \Delta \mathrm{n}_{0} \mathrm{t}_{\mathrm{k}}$ | Mean motion difference from computed value |
| $\mathrm{n}_{\mathrm{A}}=\mathrm{n}_{0}+\Delta \mathrm{n}_{\mathrm{A}}$ | Corrected Mean Motion |
| $\mathrm{M}_{\mathrm{k}}=\mathrm{M}_{0}+\mathrm{n}_{\mathrm{A}} \mathrm{t}_{\mathrm{k}}$ | Mean Anomaly |
|  | Kepler's equation ( $M_{k}=E_{k}-e \sin E_{k}$ ) solved for Eccentric anomaly $\left(E_{k}\right)$ by iteration: |
| $\mathrm{E}_{0}=\mathrm{M}_{\mathrm{k}}$ | - Initial Value (radians) |
| $E_{j}=E_{j-1}+\frac{M_{k}-E_{j-1}+e \sin E_{j-1}}{1-e \cos E_{j-1}}$ | - Refined Value, three iterations, (j=1,2,3) |
| $\mathrm{E}_{\mathrm{k}}=\mathrm{E}_{3}$ | - Final Value (radians) |
| $v_{\mathrm{k}}=2 \tan ^{-1}\left(\sqrt{\frac{1+e}{1-e}} \tan \frac{E_{k}}{2}\right)$ | True Anomaly (unambiguous quadrant) |

* $\quad \mathrm{A}_{\text {ReF }}=26,559,710$ meters
** $\mathbf{t}$ is GPS system time at time of transmission, i.e., GPS time corrected for transit time (range/speed of light). Furthermore, $\mathrm{t}_{\mathrm{k}}$ shall be the actual total difference between the time $\mathbf{t}$ and the epoch time $\mathrm{t}_{\mathrm{e} \text { e }}$, and must account for beginning or end of week crossovers. That is if $t_{k}$ is greater than 302,400 seconds, subtract 604,800 seconds from $\mathrm{t}_{\mathrm{k}}$. If $\mathrm{t}_{\mathrm{k}}$ is less than -302,400 seconds, add 604,800 seconds to $\mathrm{t}_{\mathrm{k}}$.


## IS800-949 :

## Section Number :

### 3.5.3.6.1.1-4

## WAS :

Table 3.5-2. Elements of Coordinate System (part 2 of 2)

## Redlines :

Table 3.5-2.—Elements $\theta$ Broadcast CoordinateNavigation Systemuser Equations (partsheet 2 of $z \underline{\text { ) }}$ )
IS:
Table 3.5-2. Broadcast Navigation User Equations (sheet 2 of 4)

## IS800-1009 :

Insertion after object IS800-182
Table 3.5-2. Part 2

| Element/Equation | Description |
| :---: | :---: |
|  | $\left.\begin{array}{l}\text { Argument of Latitude } \\ \text { Argument of Latitude Correction } \\ \text { Radial Correction } \\ \text { Inclination Correction }\end{array}\right\}$ <br> Second Harmonic <br> Perturbations <br> Corrected Argument of Latitude <br> Corrected Radius <br> Corrected Inclination <br> Positions in orbital plane <br> Rate of Right Ascension <br> Corrected Longitude of Ascending Node <br> Earth-fixed coordinates of SV antenna phase center |
| *** $\dot{\Omega}_{\text {REF }}=-2.6 \times 10^{-9}$ semi-circles/second. |  |

## Section Number :

### 3.5.3.6.1.1-6

WAS :
N/A

## Redlines:

<INSERTED OBJECT>
IS :
Broadcast Navigation User Equations (sheet 3 of 4)

## IS800-1011 :

Insertion after object IS800-1009 (See Previous)

## Section Number :

3.5.3.6.1.1-7

WAS :
N/A
Redlines:
<INSERTED OBJECT>
IS :
Table 3.5-2. Part 3

| Element/Equation | Description |
| :---: | :---: |
| SV Velocity |  |
| $\dot{E}_{\mathrm{k}}=\mathrm{n} /\left(1-\mathrm{ecos} \mathrm{E}_{\mathrm{k}}\right)$ | Eccentric Anomaly Rate |
| $\dot{v}_{k}=\dot{\mathrm{E}}_{\mathrm{k}} \sqrt{1-e^{2}} /\left(1-e \cos E_{k}\right)$ | True Anomaly Rate |
| $\begin{aligned} & \left(d i_{k} / d t\right)=(\text { IDOT })+2 \dot{v}_{k}\left(\mathrm{c}_{\text {is }} \cos 2 \phi_{\mathrm{k}}-\mathrm{c}_{\mathrm{ic}} \sin \right. \\ & \left.2 \phi_{\mathrm{k}}\right) \end{aligned}$ | Corrected Inclination Angle Rate |
| $\dot{u}_{\mathrm{k}}=\dot{v}_{k}+2 \dot{v}_{k}\left(\mathrm{cus}_{\text {us }} \cos 2 \phi_{\mathrm{k}}-\mathrm{c}_{\text {uc }} \sin 2 \phi_{\mathrm{k}}\right)$ | Corrected Argument of Latitude Rate |
| $\dot{r}_{k}=\mathrm{eAE} \dot{E}_{\mathrm{k}} \sin \mathrm{Ek}+2 \dot{v}_{k}\left(\mathrm{c}_{\mathrm{rs}} \cos 2 \phi_{\mathrm{k}}-\mathrm{c}_{\mathrm{rc}} \sin 2 \phi_{\mathrm{k}}\right)$ | Corrected Radius Rate |
| $\dot{\Omega}_{\mathrm{k}}=\dot{\Omega}-\dot{\Omega}_{\mathrm{e}}$ | Longitude of Ascending Node Rate |
| $\dot{\mathrm{x}}_{k}^{\prime}=\dot{r}_{k} \cos \mathrm{u}_{\mathrm{k}}-r_{k} \dot{\mathrm{u}}_{\mathrm{k}} \sin \mathrm{u}_{\mathrm{k}}$ | In- plane $x$ velocity |
| $\dot{y}_{k}^{\prime}=\dot{r}_{k} \sin \mathrm{u}_{\mathrm{k}}+r_{k} \dot{\mathrm{u}}_{\mathrm{k}} \cos \mathrm{u}_{\mathrm{k}}$ | In- plane $y$ velocity |
| $\begin{array}{r} \dot{x}_{\mathrm{k}}=-x_{k}^{\prime} \dot{\Omega}_{\mathrm{k}} \sin \Omega_{\mathrm{k}}+\dot{x}_{k}^{\prime} \cos \Omega_{\mathrm{k}}-\dot{y}_{k}^{\prime} \sin \Omega_{\mathrm{k}} \cos \mathrm{i}_{\mathrm{k}} \\ \\ -y_{k}^{\prime}\left(\dot{\Omega}_{\mathrm{k}} \cos \Omega_{\mathrm{k}} \cos i_{\mathrm{k}}-\left(d i_{k} / d t\right) \sin \Omega_{\mathrm{k}} \sin \mathrm{i}_{\mathrm{k}}\right) \end{array}$ | Earth- Fixed $x$ velocity (m/s) |
| $\begin{aligned} \dot{y}_{\mathrm{k}} & =x_{k}^{\prime} \dot{\Omega}_{\mathrm{k}} \cos \Omega_{\mathrm{k}}+\dot{x}_{k}^{\prime} \sin \Omega_{\mathrm{k}}+\dot{y}_{k}^{\prime} \cos \Omega_{\mathrm{k}} \cos \mathrm{i}_{\mathrm{k}} \\ & -y_{k}^{\prime}\left(\dot{\Omega}_{\mathrm{k}} \sin \Omega_{\mathrm{k}} \cos \mathrm{i}_{\mathrm{k}}+\left(d i_{k} / d t\right) \cos \Omega_{\mathrm{k}} \sin \mathrm{i}_{\mathrm{k}}\right) \end{aligned}$ | Earth- Fixed $y$ velocity (m/s) |
| $\dot{z}_{\mathrm{k}}=\dot{y}_{k}^{\prime} \sin \mathrm{i}_{\mathrm{k}}+y_{k}^{\prime}\left(d i_{k} / d t\right) \cos \mathrm{i}_{\mathrm{k}}$ | Earth- Fixed z velocity (m/s) |

## IS800-1008 :

Insertion after object IS800-1011 (See Previous)
Section Number :
3.5.3.6.1.1-8

WAS :
N/A
Redlines:
<INSERTED OBJECT>
IS :
Table 3.5-2. Broadcast Navigation User Equations (sheet 4 of 4)

## IS800-1010 :

Insertion after object IS800-1008 (See Previous)

## Section Number :

3.5.3.6.1.1-9

WAS :
N/A
Redlines:
<INSERTED OBJECT>
IS :
Table 3.5-2. Part 4

| Element/Equation | Description |
| :---: | :---: |
| SV Acceleration |  |
| $\mathrm{R}_{\mathrm{E}}=6378137.0$ meters | WGS 84 Earth Equatorial Radius |
| $\mathrm{J}_{2}=0.0010826262$ | Oblate Earth Gravity Coefficient |
| $\mathrm{F}=-(3 / 2) \mathrm{J}_{2}\left(\mu / r_{k}^{2}\right)\left(\mathrm{R}_{\mathrm{E}} / r_{\mathrm{k}}\right)^{2}$ | Oblate Earth acceleration Factor |
| $\begin{aligned} & \ddot{x}_{k}=-\mu\left(x_{k} / r_{k}^{3}\right)+\mathrm{F}\left[\left(1-5\left(z_{k} / r_{k}\right)^{2}\right)\left(x_{k} / r_{k}\right)\right] \\ &+2 \dot{y}_{k} \dot{\Omega}_{e}+x_{k} \dot{\Omega}_{e}^{2} \end{aligned}$ | Earth- Fixed $x$ acceleration (m/s ${ }^{2}$ ) |
| $\begin{aligned} & \ddot{y}_{k}=-\mu\left(y_{k} / r_{k}^{3}\right)+\mathrm{F}\left[\left(1-5\left(z_{k} / r_{k}\right)^{2}\right)\left(y_{k} / r_{k}\right)\right] \\ &-2 \dot{x}_{k} \dot{\Omega}_{e}+y_{k} \dot{\Omega}_{e}^{2} \end{aligned}$ | Earth- Fixed $y$ Acceleration (m/s ${ }^{2}$ ) |
| $\ddot{z}_{k}=-\mu\left(z_{k} / r_{k}^{3}\right)+\mathrm{F}\left[\left(3-5\left(z_{k} / r_{k}\right)^{2}\right)\left(z_{k} / r_{k}\right)\right]$ | Earth- Fixed z Acceleration (m/s ${ }^{2}$ ) |

## Section Number :

### 6.3.3.0-1

WAS :
As an aid to user equipment receiver designers, a plot is provided (Figure 6-1) of a typical GPS III phase noise spectral density for the un-modulated L1C carrier.

## Redlines :

As an aid to user equipment receiver designers, a plot is provided (Figure 6-1) of a typical GPS III and GPS IIIF phase noise spectral density for the un-modulated L1C carrier.

IS :
As an aid to user equipment receiver designers, a plot is provided (Figure 6-1) of a typical GPS III and GPS IIIF phase noise spectral density for the un-modulated L1C carrier.

## IS800-1007 :

## Section Number :

6.3.3.0-1.0-2

## WAS :

Figure 6-1 Typical GPS III L1C Carrier Phase Noise Spectral Density

## Redlines :

Figure 6-1 Typical GPS III and GPS IIIF L1C Carrier Phase Noise Spectral Density
IS:
Figure 6-1 Typical GPS III and GPS IIIF L1C Carrier Phase Noise Spectral Density

